

“New” errors in Nino 3.4 forecasts

Michael Tippett
Columbia University

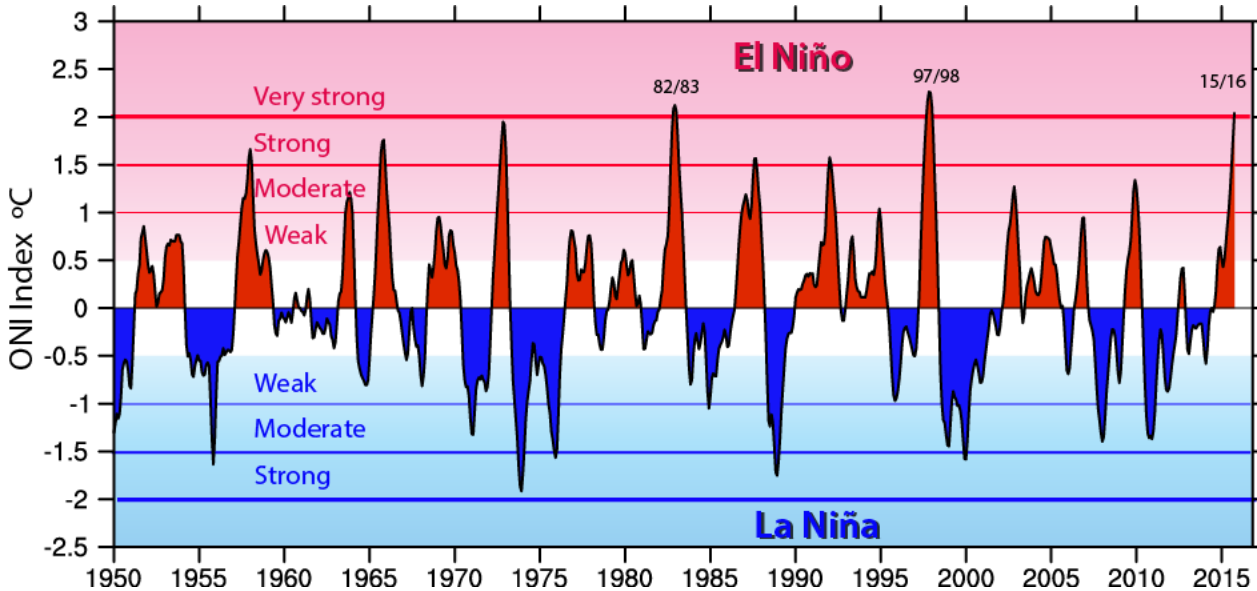
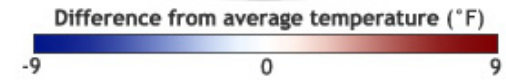
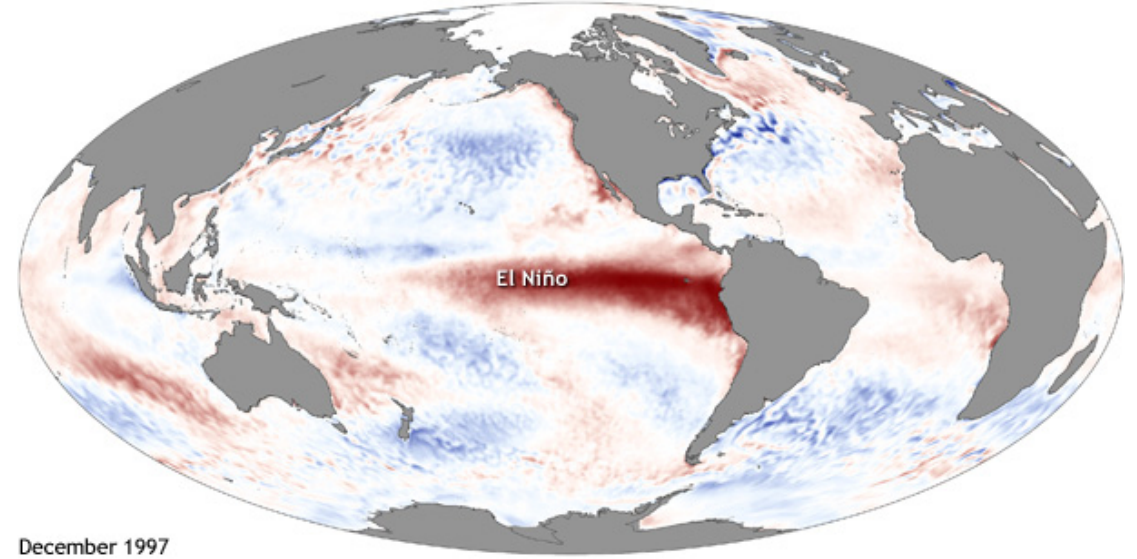
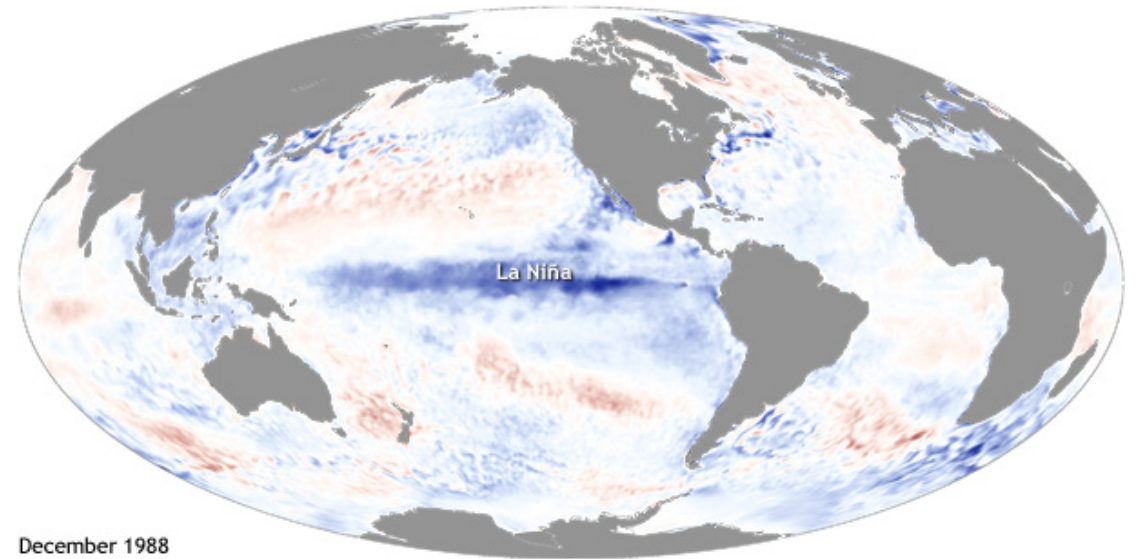
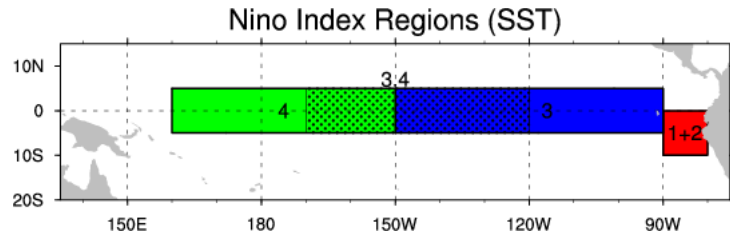
Michelle L’Heureux, Arun Kumar, and Emily Becker
NOAA/NWS/NCEP/Climate Prediction Center

Summary

- Late-spring ENSO *forecasts errors* depend on the observed ENSO tendency before the forecast.
 - “Momentum” = ENSO tends to keep going in the same direction
 - Models have state-dependent errors
- Consequence: Late-spring ENSO forecasts are unreliable.
- Are model dynamics or initialization to blame?
 - Some evidence for dynamics being the culprit
- EOF analysis shows ENSO time structure is 2-dimensional
 - Models with better time structure have smaller errors.
 - EOF-based regression reduces forecast MSE

What is ENSO?

- El Niño, La Niña, and Niño 3.4*



*No flavors today

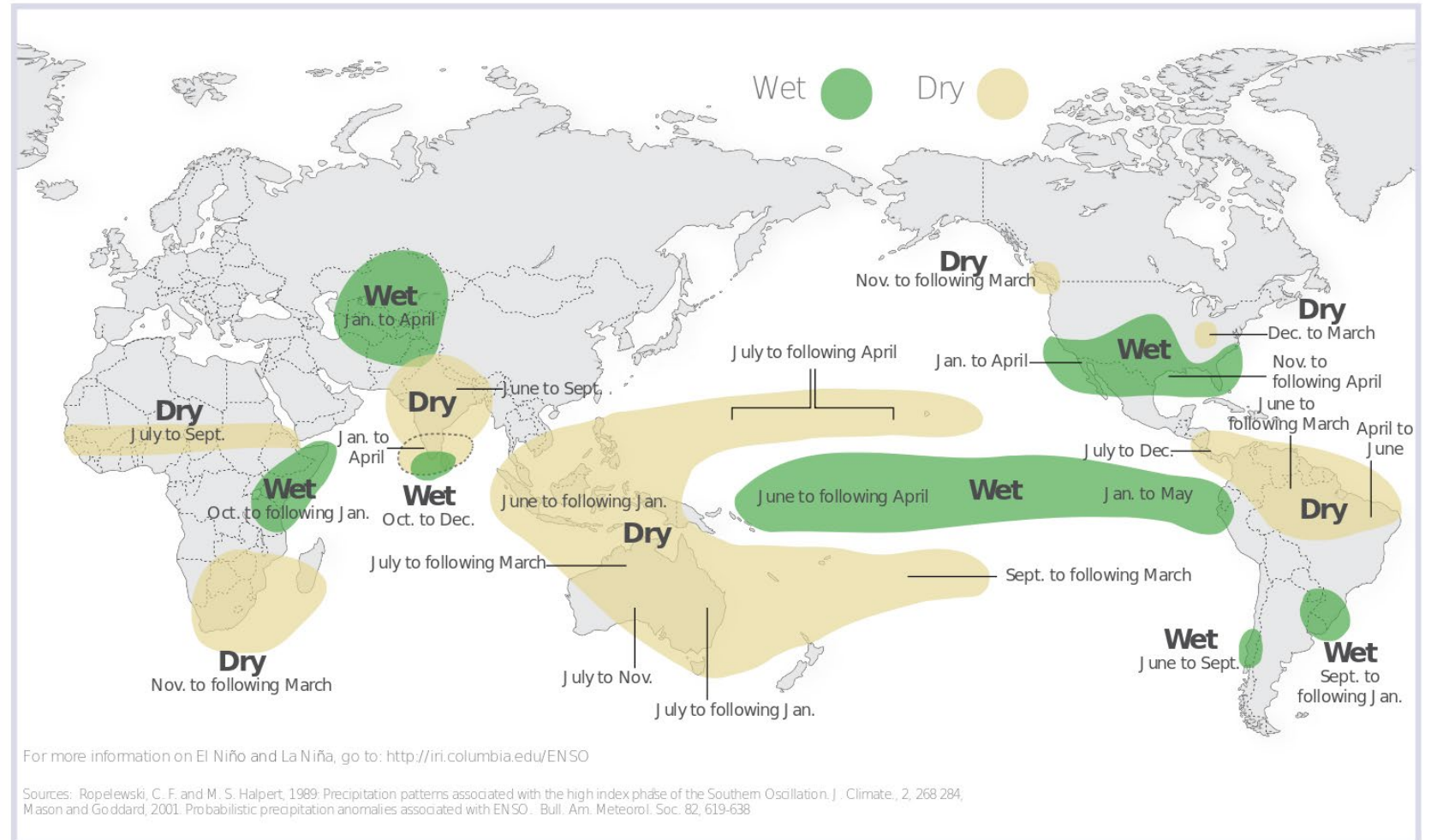
Why is ENSO is important?

Predictable impacts

Temperature, precipitation, hurricanes, tornadoes, human conflict ...

El Niño and Rainfall

El Niño conditions in the tropical Pacific are known to shift rainfall patterns in many different parts of the world. Although they vary somewhat from one El Niño to the next, the strongest shifts remain fairly consistent in the regions and seasons shown on the map below.



“El Niño's effects on Europe are controversial, complex and difficult to analyze, as it is one of several factors that influence the weather over the continent and other factors can overwhelm the signal.” Wikipedia

How is ENSO predicted?

Main forecast guidance:

- Initialized coupled atmosphere-ocean models
 - Systematic errors (biases) are removed

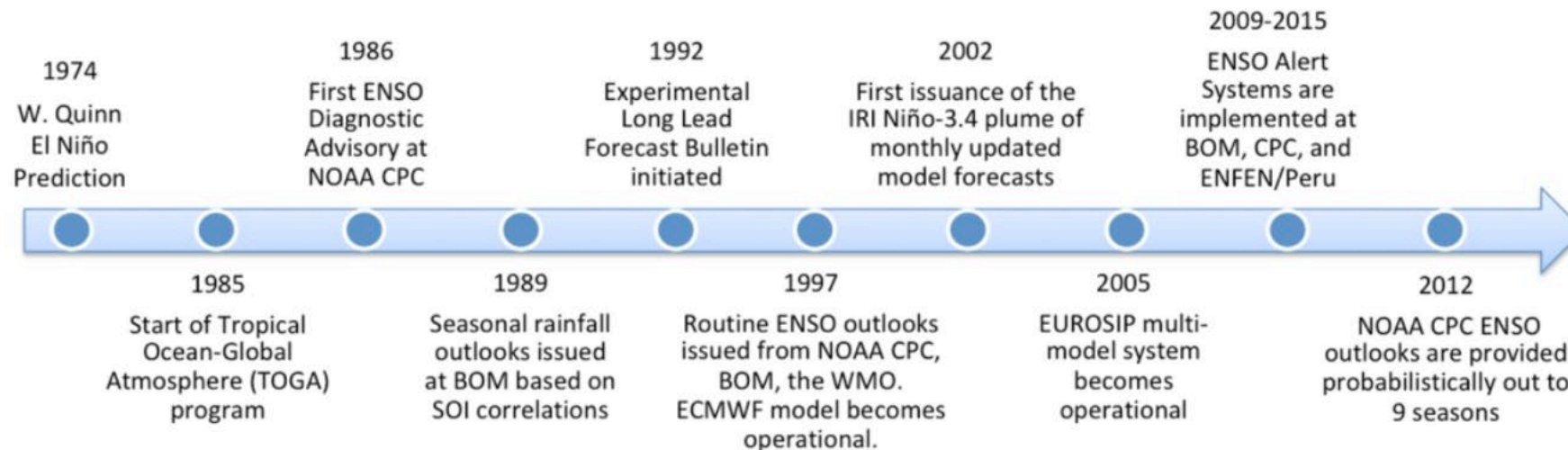
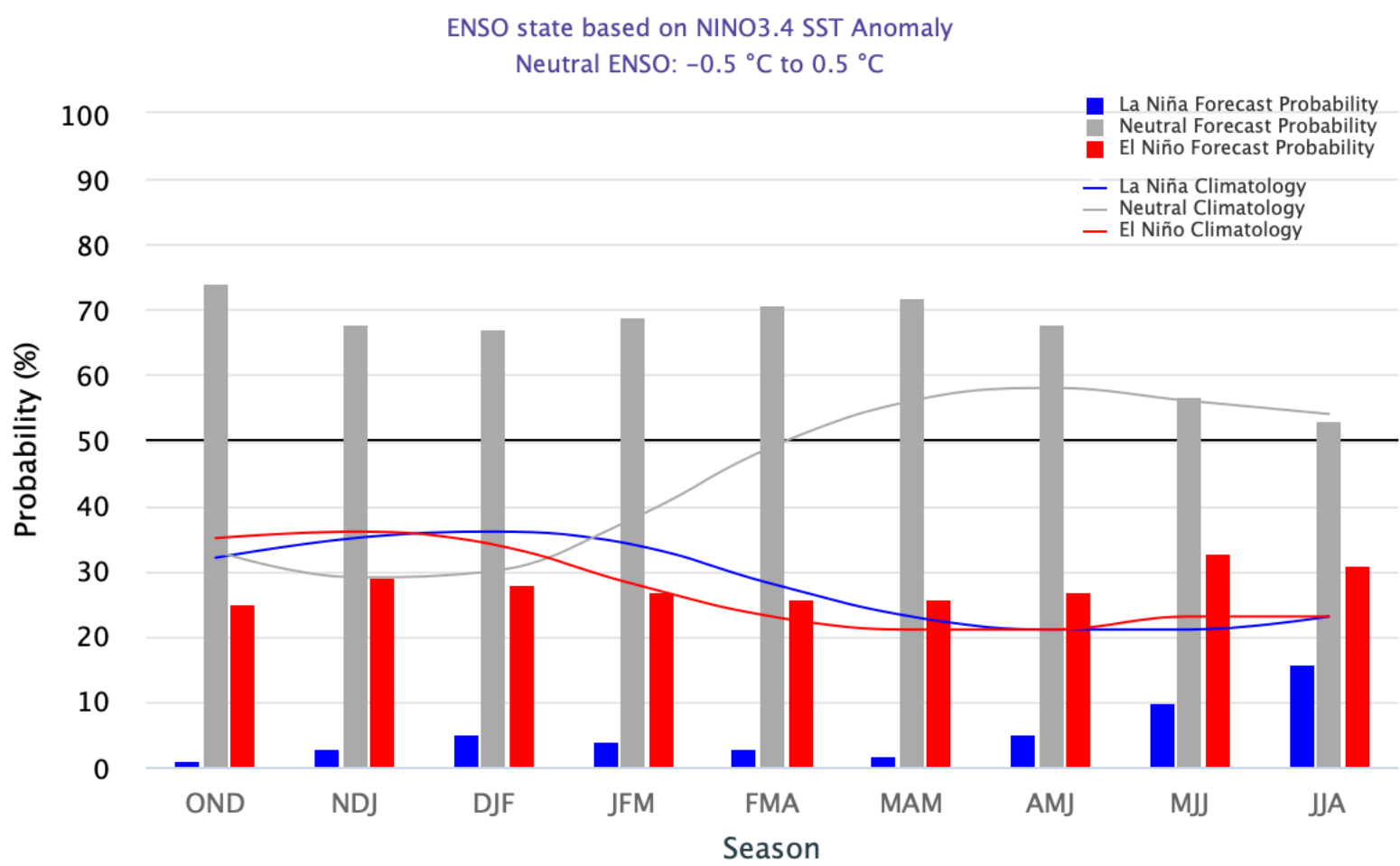


Figure 1. A timeline of events in ENSO forecasting.

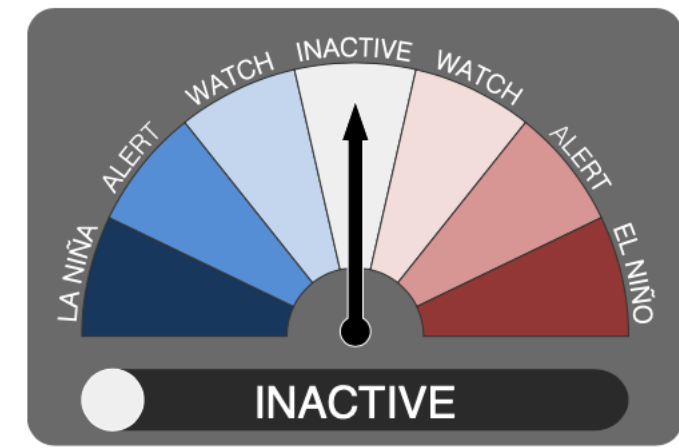
Categorical

What do ENSO forecasts look like?

IRI/NOAA Mid-October 2019 IRI/CPC Model-Based Probabilistic ENSO Forecasts



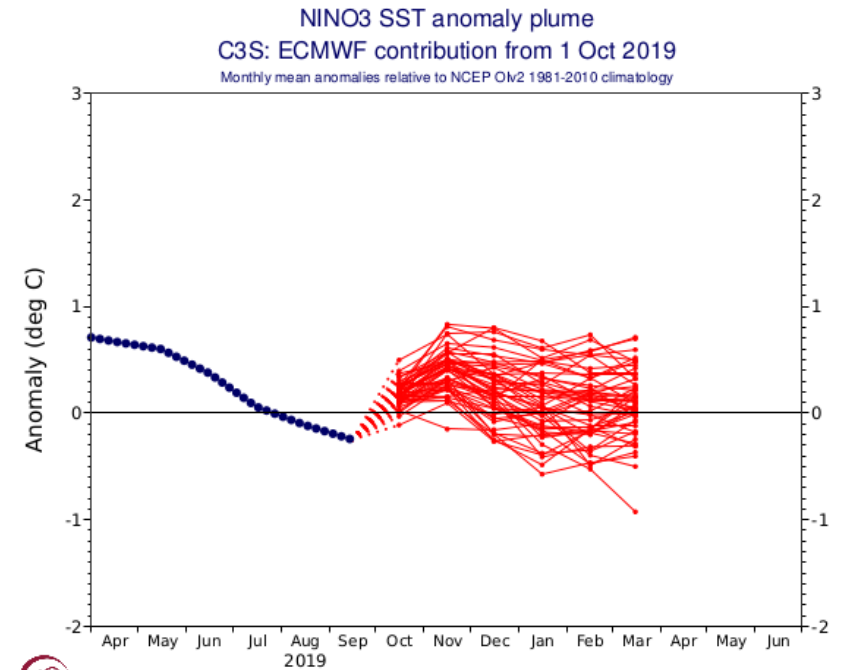
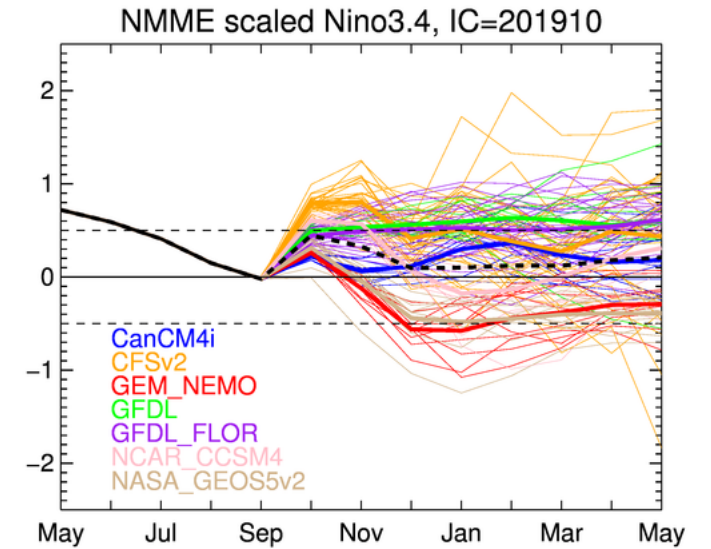
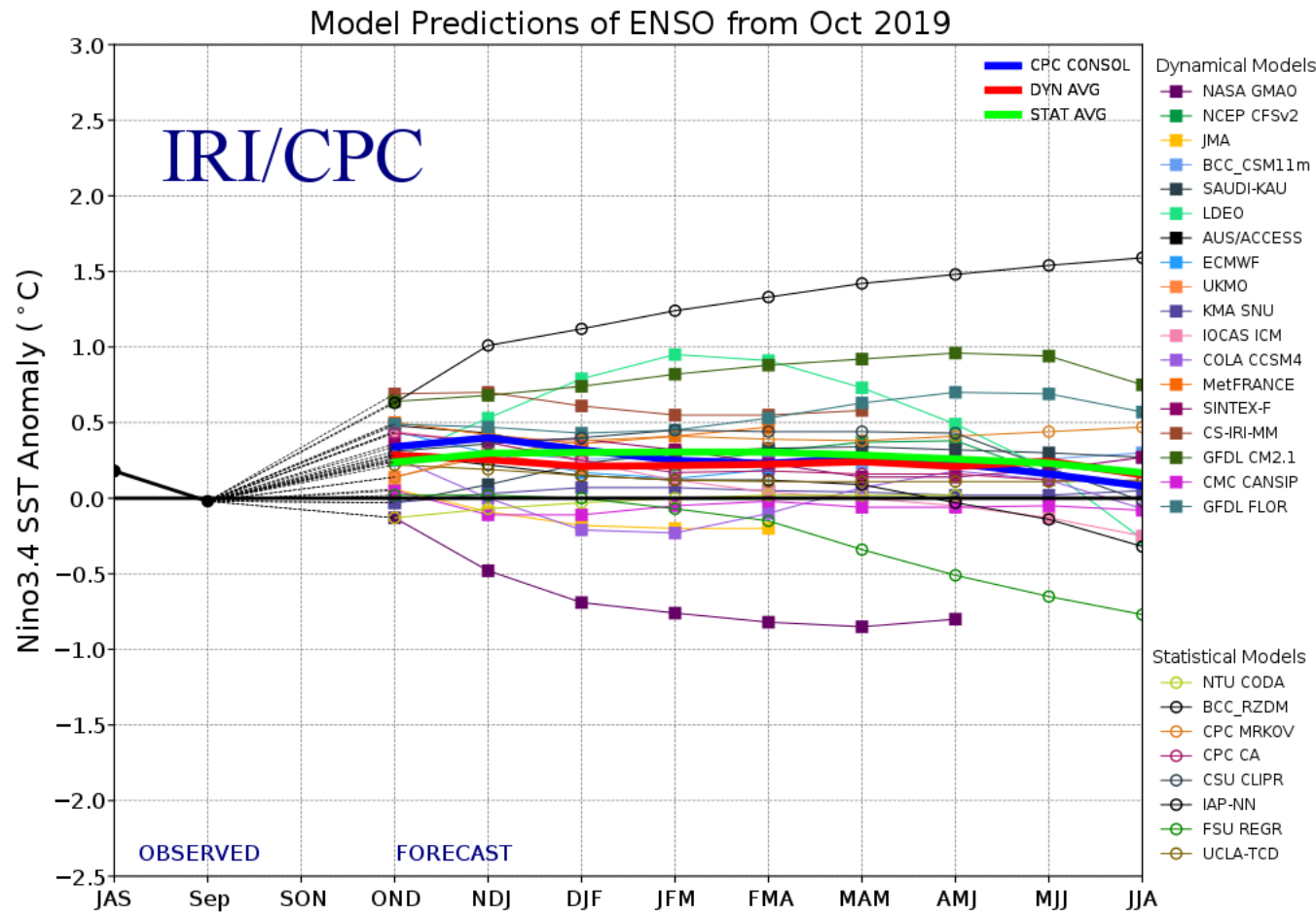
BoM



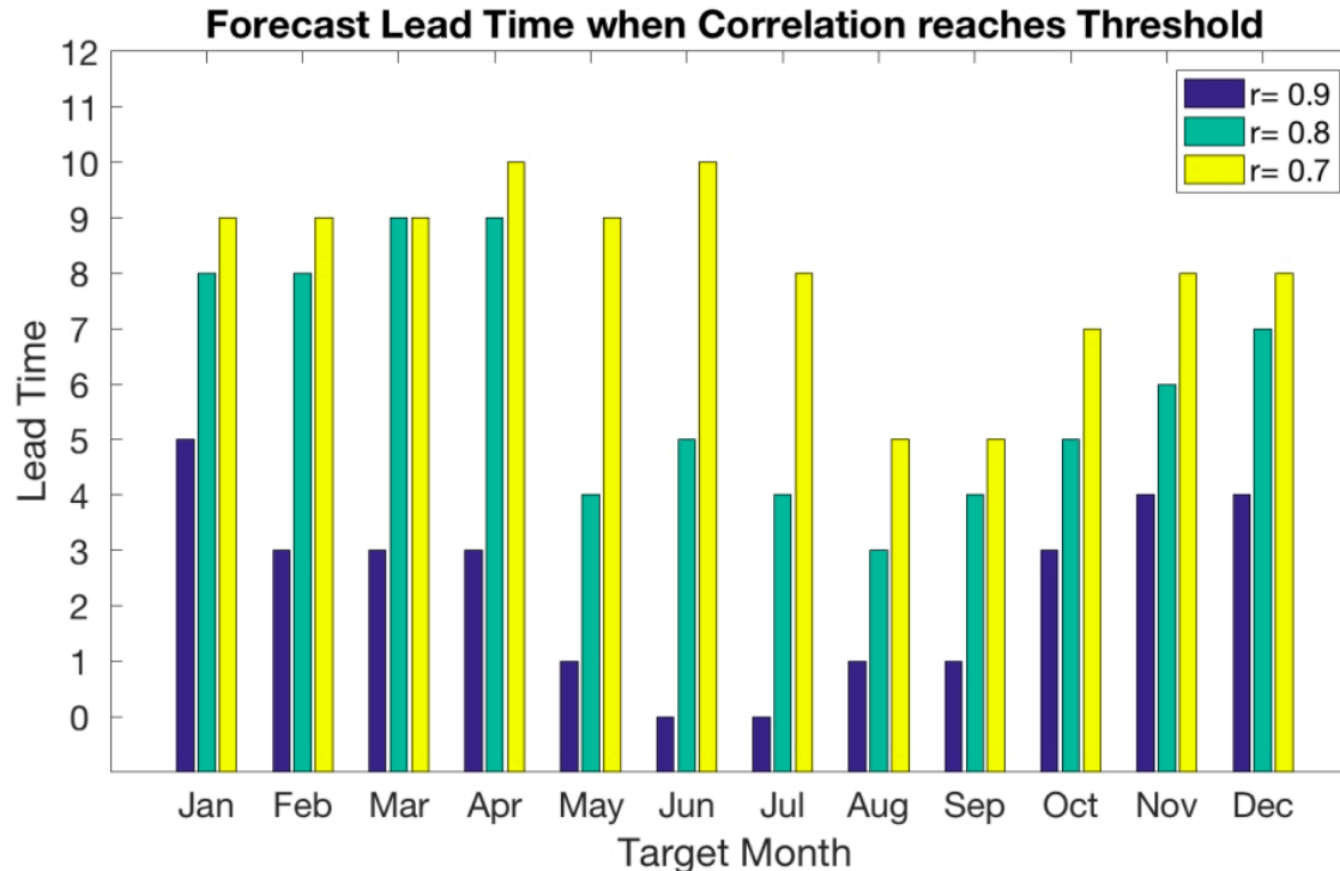
JMA

YEAR	MONTH	mean period	El Niño (%)	ENSO neutral (%)	La Niña (%)
2019	AUG	JUN2019–OCT2019	0	100	0
	SEP	JUL2019–NOV2019	0	100	0
	OCT	AUG2019–DEC2019	0	90	10
	NOV	SEP2019–JAN2020	10	70	20
	DEC	OCT2019–FEB2020	10	70	20
2020	JAN	NOV2019–MAR2020	20	60	20
	FEB	DEC2019–APR2020	20	60	20

What do ENSO forecasts look like?



How skillful are ENSO predictions?

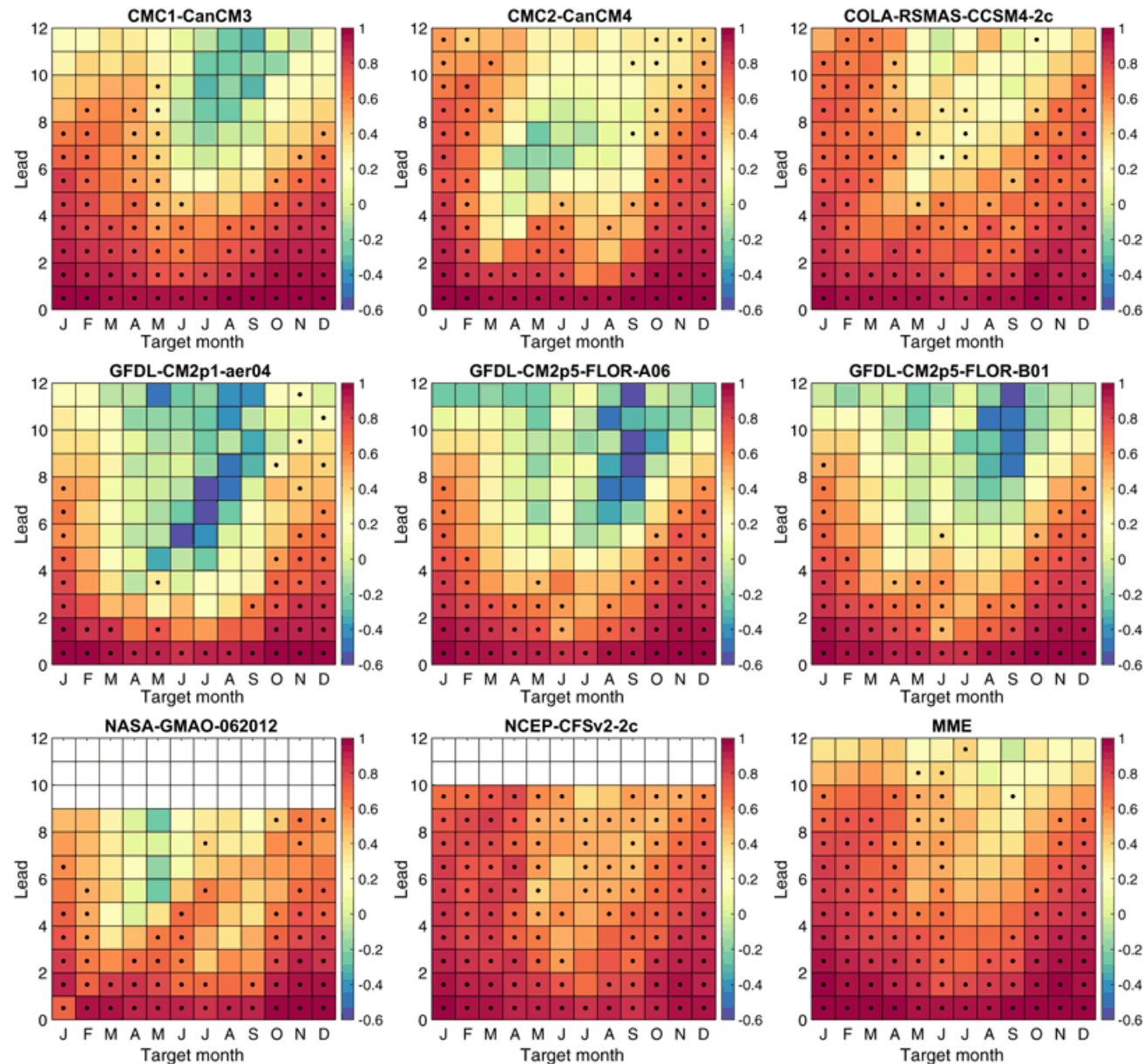


L'Heureux, M., A. Levine, M. Newman, C. Ganter, J.-J. Luo, M. Tippett, and T. Stockdale, 2019: "ENSO Prediction". In *El Niño-Southern Oscillation (ENSO) in a Changing Climate*, M. McPhaden, A. Santoso, W. Cai, eds, in press.

Figure 3. The forecast lead-time (y-axis) when Niño-3.4 index skill exceeds certain correlation thresholds. On the x-axis, the target month of the forecast is presented. Model data is based on the ensemble average of ~100 members from the North American Multi-Model Ensemble from 1982 to 2018. Departures in the Niño-3.4 index are based on 1982-2010 monthly averages.

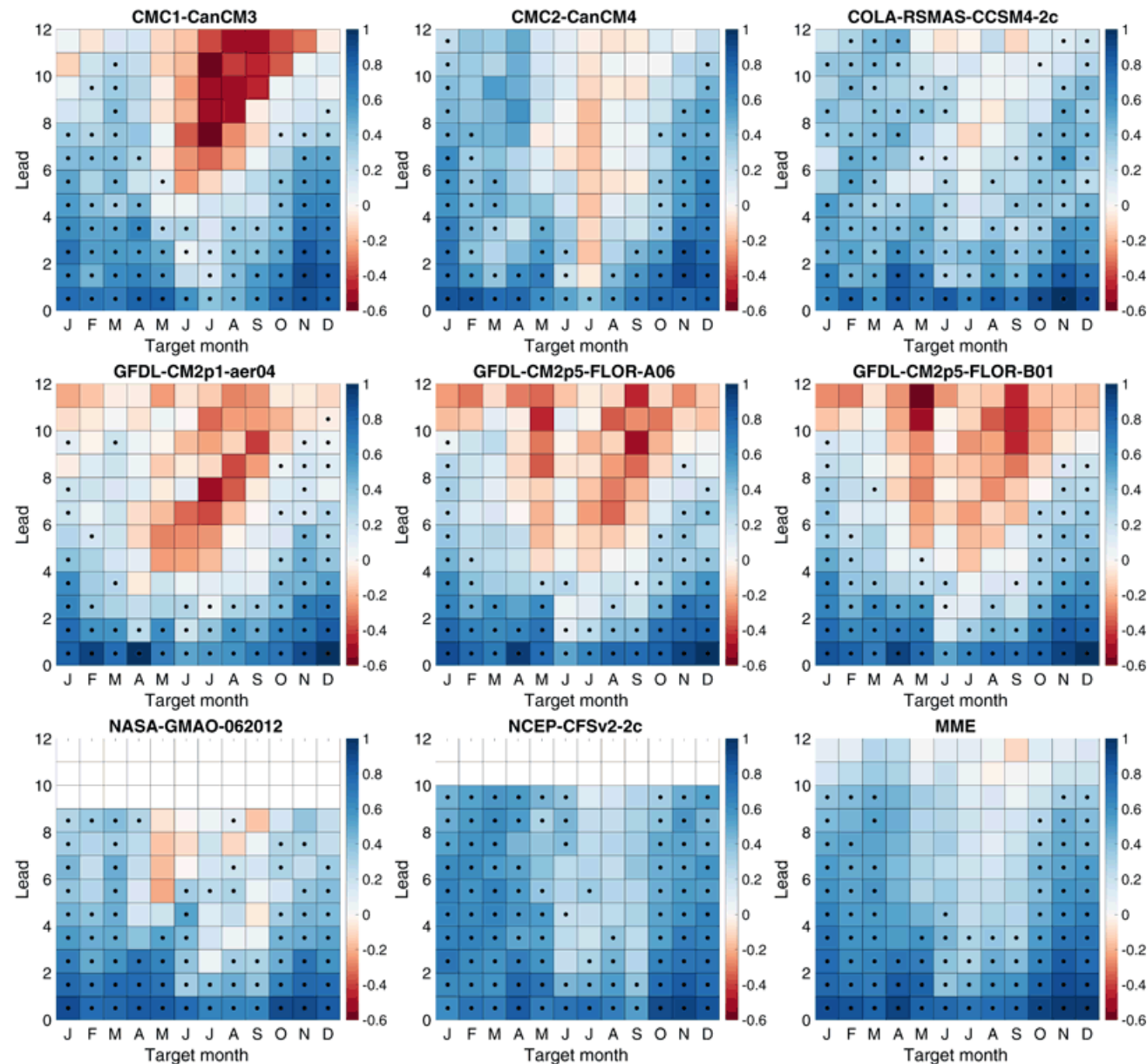
“The spring barrier causes forecasts that traverse the months of April through June to tend to have less favorable verification than those that do not go through those months.”

Mean-squared error skill score for the NMME

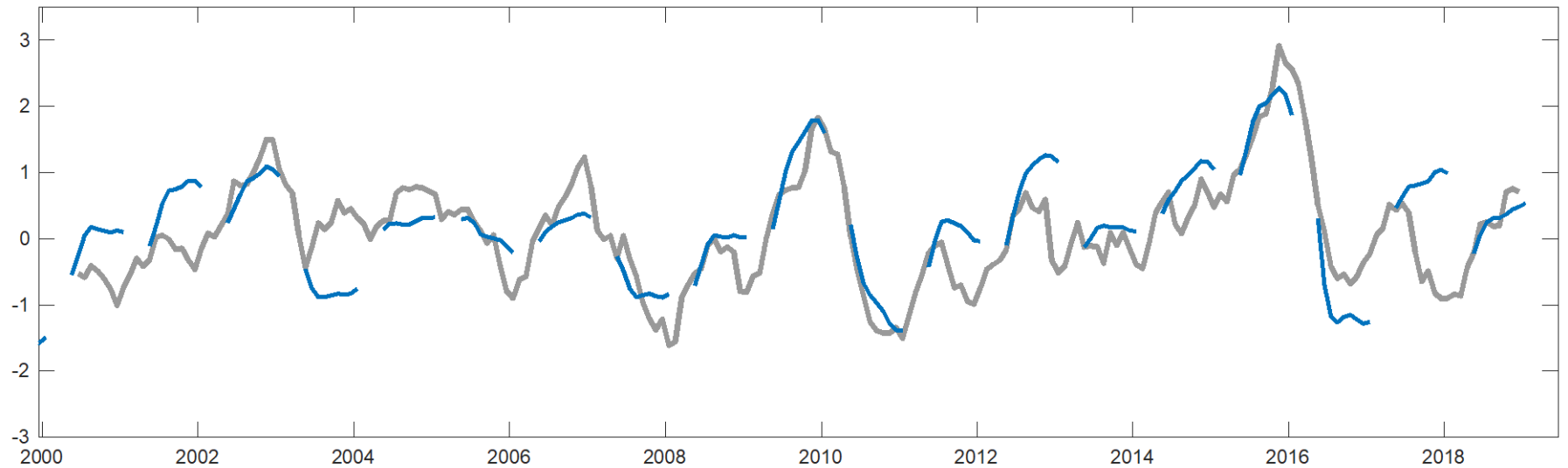
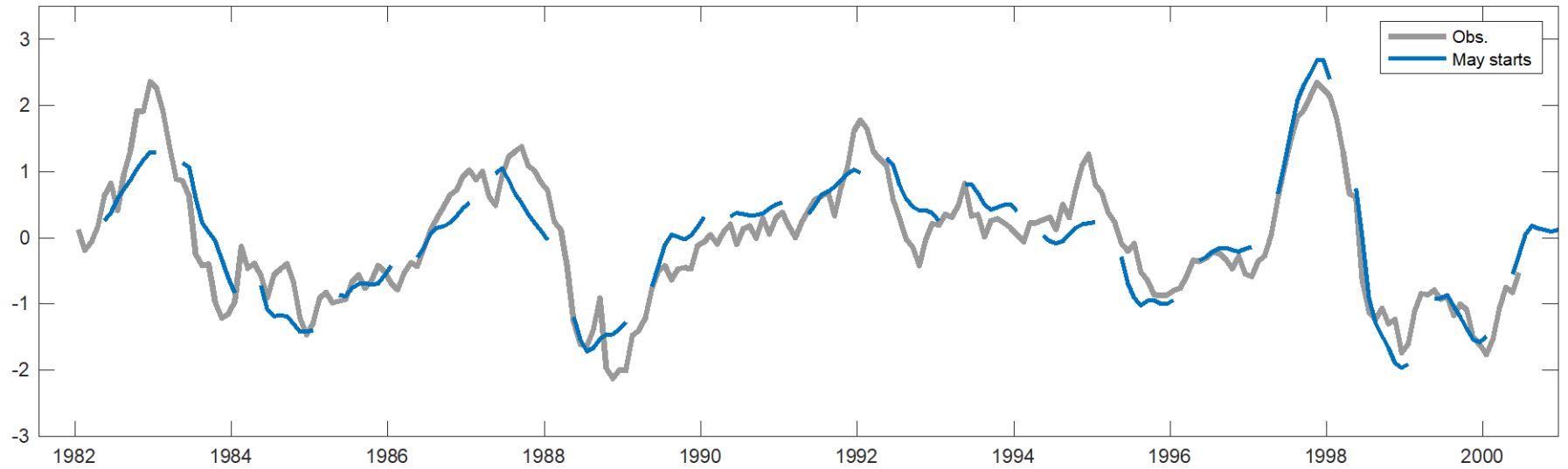


“The spring barrier causes forecasts that traverse the months of April through June to tend to have less favorable verification than those that do not go through those months.”

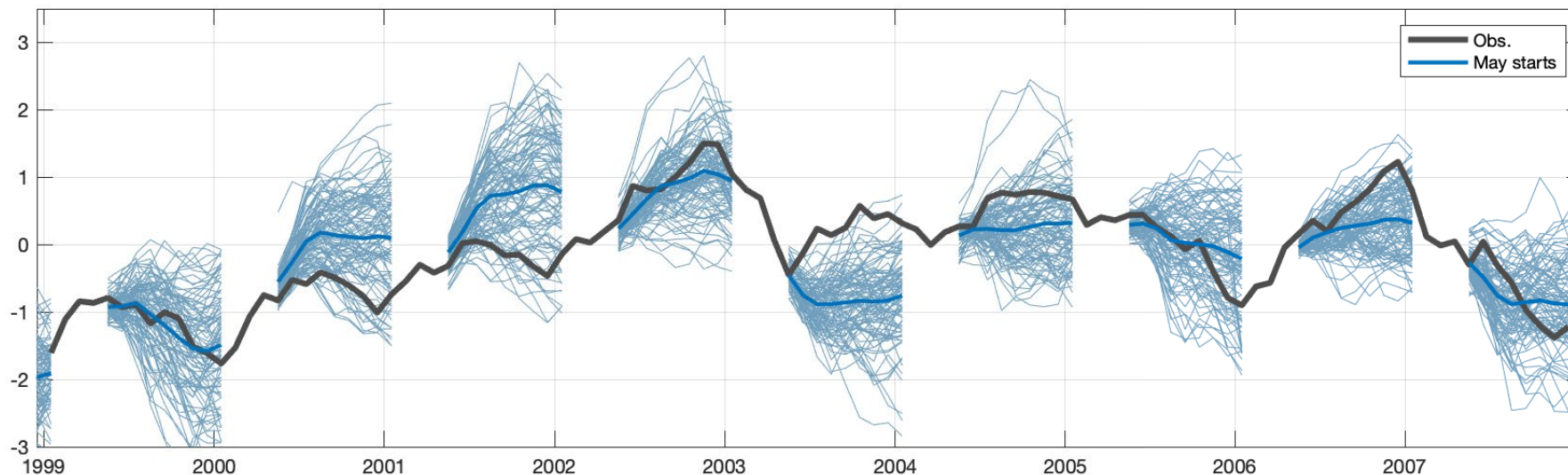
Rank probability skill score for the NMME



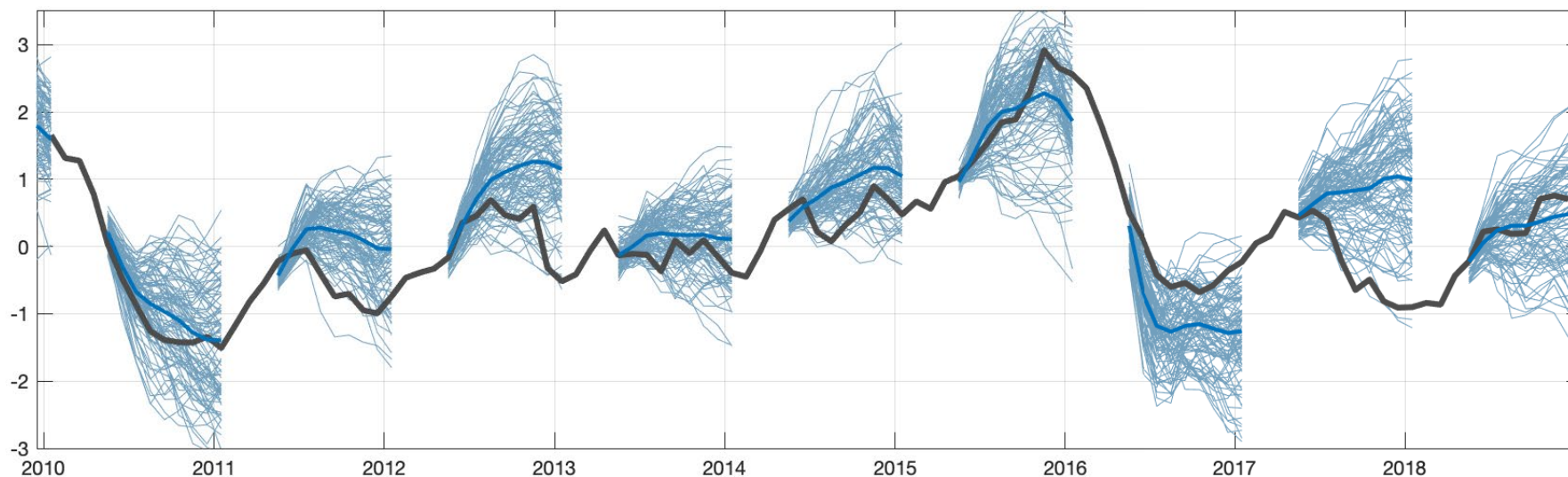
Nino 3.4 and
May NMME
ensemble-mean
forecasts
1982—2018



Nino 3.4 and
May NMME
ensemble
forecasts
1999—2018



Doesn't
look great
when the
observed
and forecast
trajectories
part ways



100 members

Is something wrong with these forecasts?

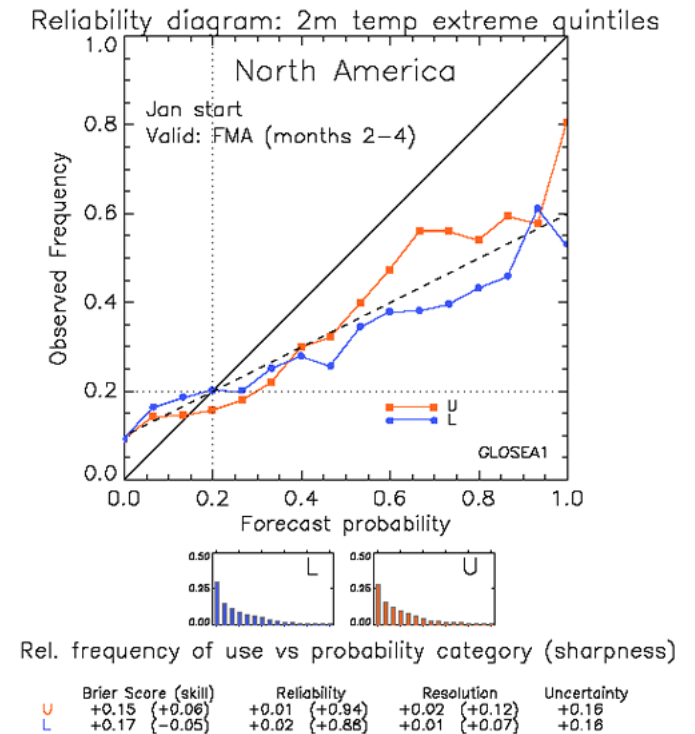
- Skill is low for spring forecasts.
 - Is this what low skill looks like?
- What does it mean for a probabilistic forecast to be wrong?
- Wrong = uncalibrated
 - Unreliable probabilities
 - Forecast ensemble that is is:
 - Over-dispersed (under-confident)
 - Under-dispersed (over-confident)
 - Biased

Focus on forecast tendencies

- Define the ***forecast tendency*** as lead-4 minus lead-1
 - For a Apr start, forecast tendency = Jul forecast – Apr forecast
 - For a May start, forecast tendency = Aug forecast – May forecast
- Compare forecast tendencies with observed ones
- Two forecast quantities
 - Sign of the tendency
 - “The probability of the tendency being positive is 90%”
 - Value of the tendency
 - The forecast distribution (pdf) of tendency values
- Are forecast tendencies reliable?

What does it mean for forecast *probabilities* to be reliable?

- (We have to look at many forecasts)
- When I forecast that the probability of an event (e.g., positive tendency) is X%, it occurs X% of the time.
- $E[O | F] = F$
 - O is 1 when the event occurs and 0 otherwise
 - F is the forecast probability
 - E means expectation (average)
- The graph of $E[O | F]$ vs. F is called a reliability diagram



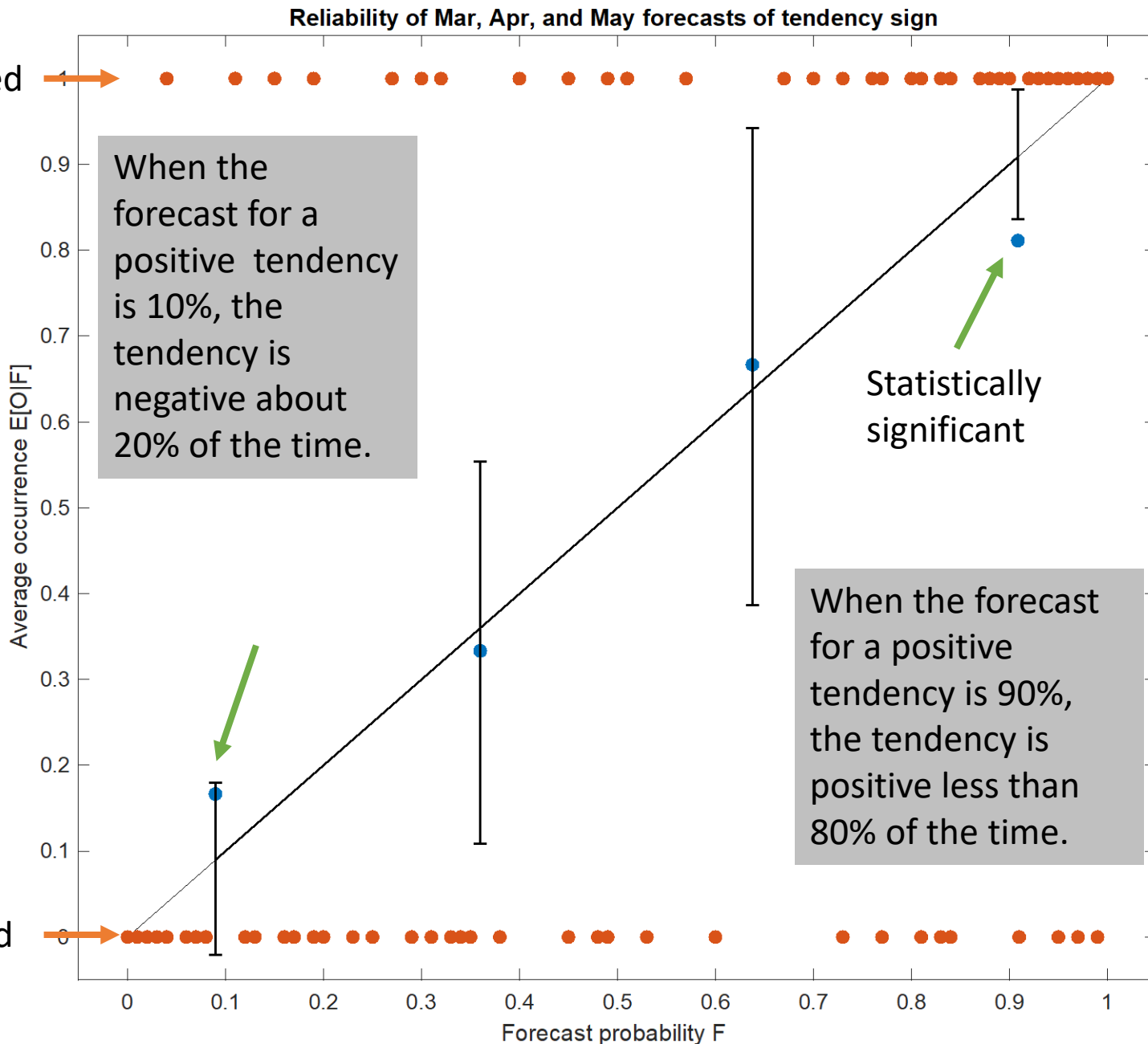
Mar, Apr,
May NMME
forecasts of
the sign of
the ENSO
tendency

Reliability diagram for
forecasts that the probability
that the sign of the tendency
will be *positive*

Reliable?

Negative tendency occurred

Positive tendency occurred

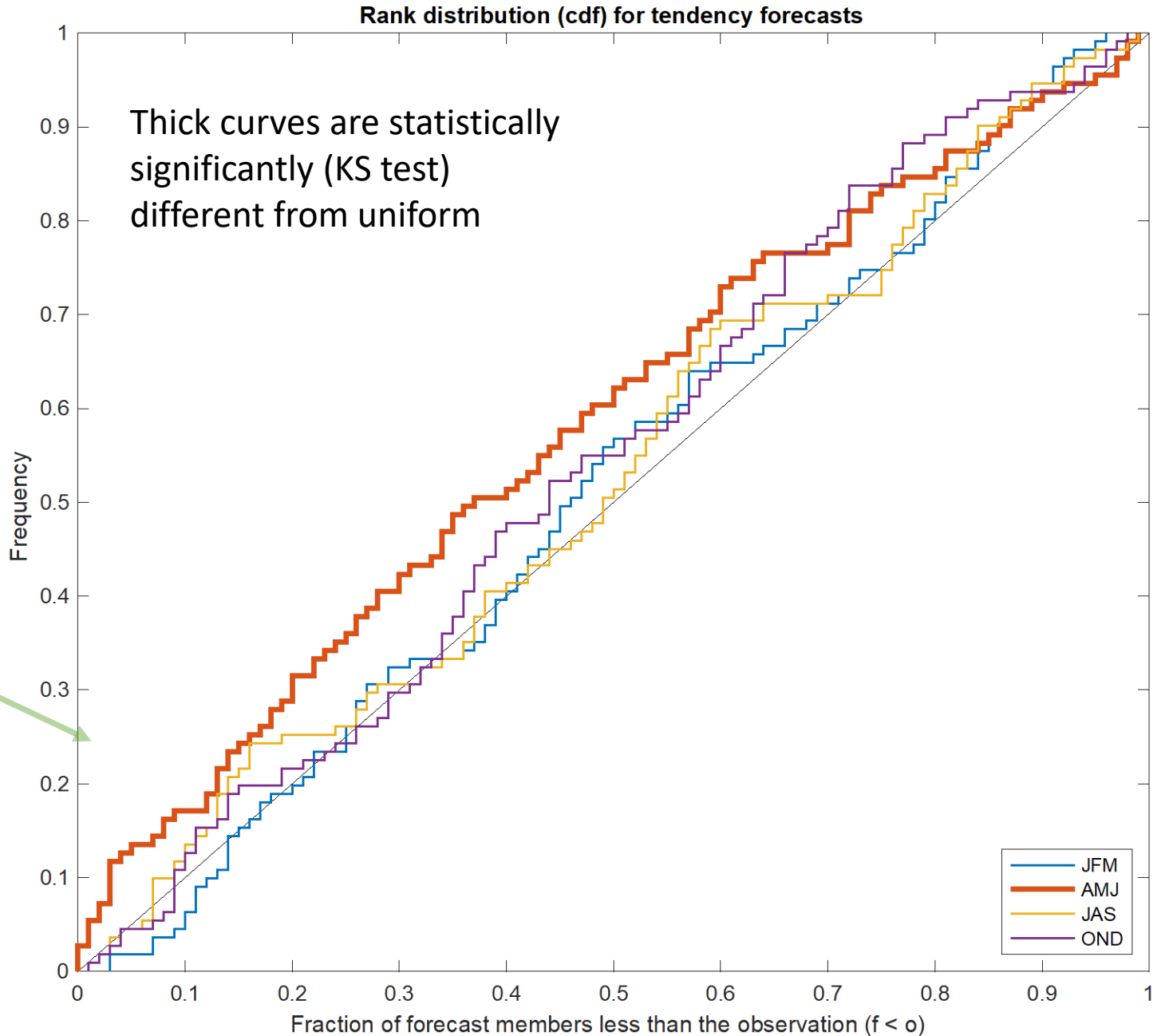
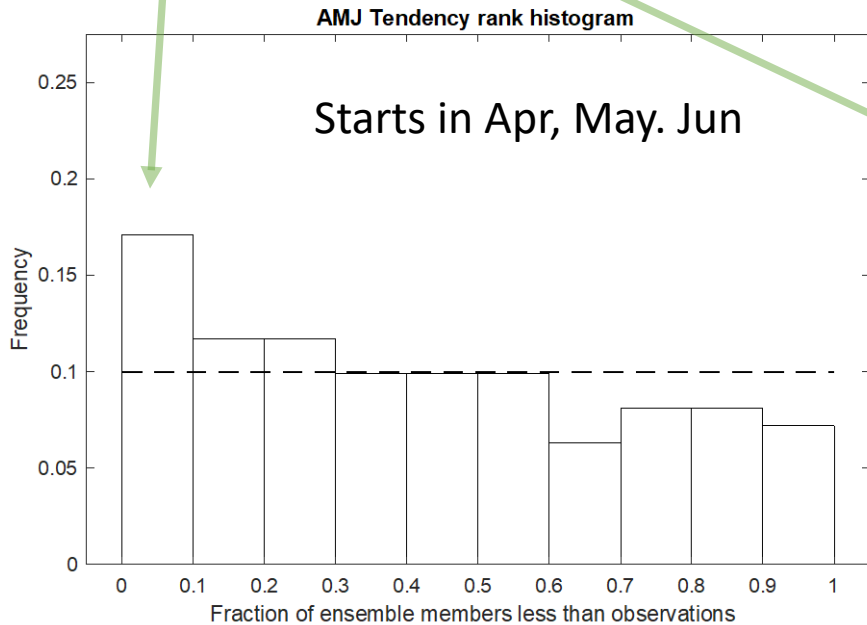


What does it mean for a forecast *ensemble* to be reliable?

- (We have to look at many forecasts)
- The observation (tendency value) is indistinguishable from a forecast ensemble member
 - The climatological distribution is a no-skill reliable forecast
- Rank histograms
 - The rank of the observations is uniformly distributed
 - If the observation value is less than all the ensemble values, its rank is 1.
 - If the observation value is greater than all the ensemble values, its rank is 101.
 - If the observation value is in the middle of the ensemble values, its rank is 51.
 - Divide rank by ensemble size = fraction of ensemble members less than observed
- On average, X% of the members should be less than the observations X% of the time.

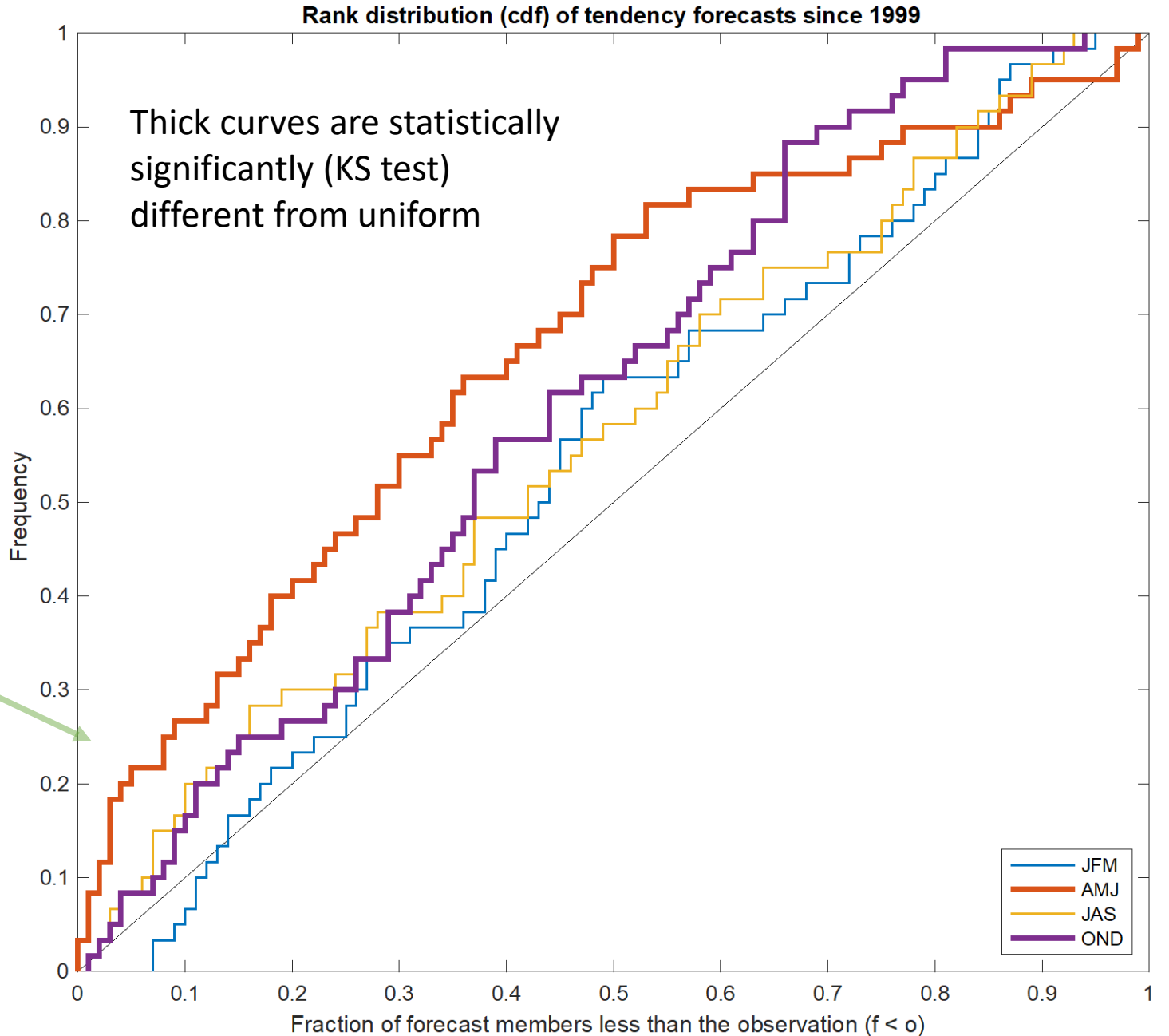
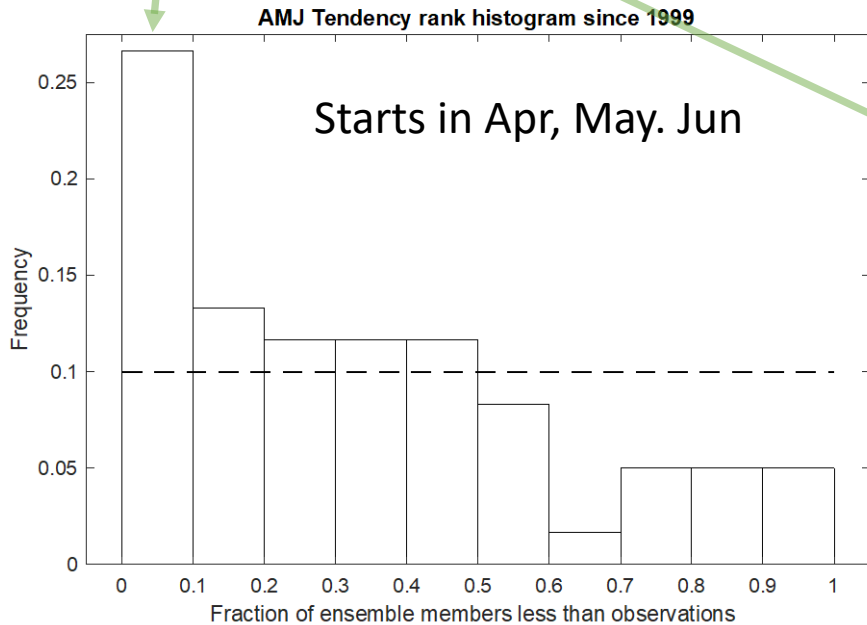
When the ensemble lies mostly above the observation, the fraction of ensemble members less than the observation is small.

The fraction of ensemble members less than the observation is small too often, which means the ensemble lies above the observation too often



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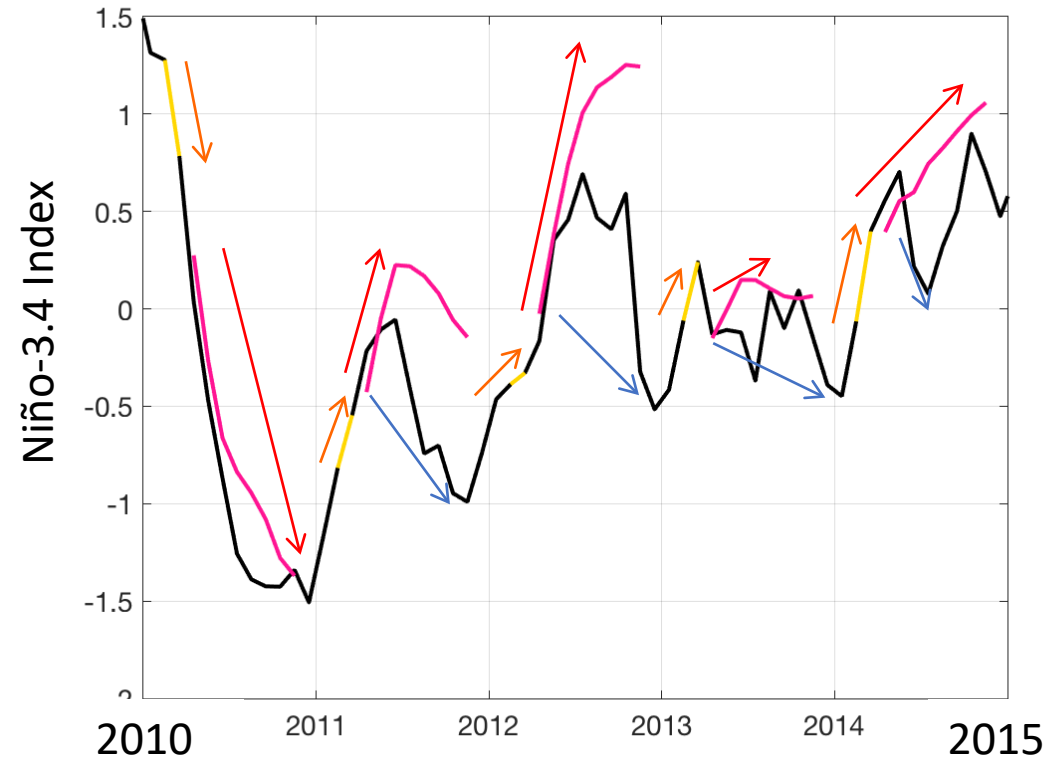
Key insight from
ENSO forecasters
Emily Becker and
Michelle L'Heureux:

“Momentum”

In the last decade, we’ve experienced several “False Alarms” when the objective model guidance over-forecasted the chances of an ENSO event (especially forecasts made in **the spring**).

Niño-3.4 SST Index

NMME initialized in May (pink) and Observations (black & March-April in yellow)



Forecasters don't “feel”
average skill. They feel
individual forecasts,
especially busts.

We want to objectively define these false alarms and have chosen the “Niño-3.4 tendency” to quantify them (not the only way).

Do models have too much “momentum” coming out of spring?

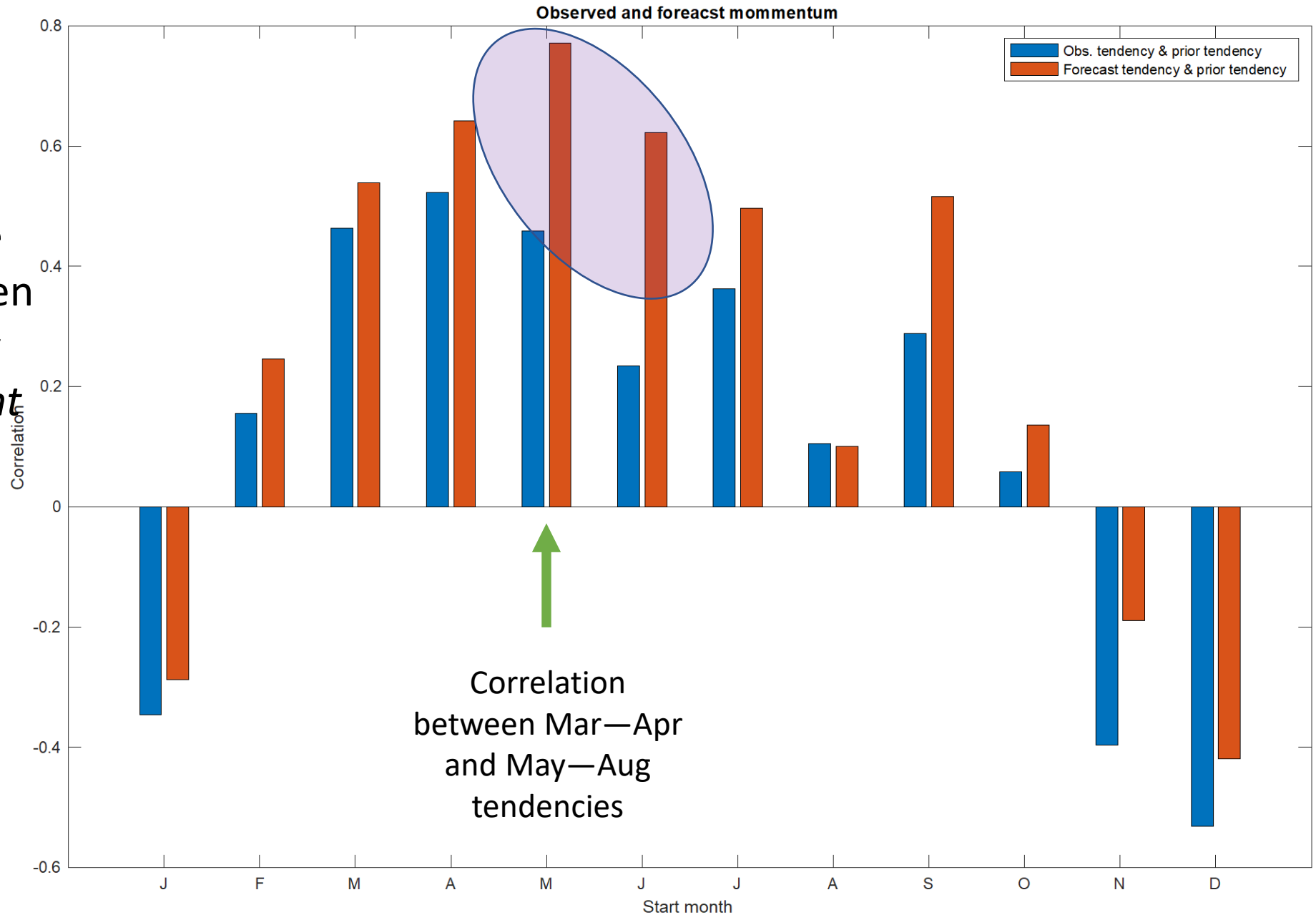
The forecast tendency follows the prior tendency too strongly



The past decade hasn't been favorable to momentum-investing approaches. ILLUSTRATION: JASON SCHNEIDER FOR THE WALL STREET JOURNAL

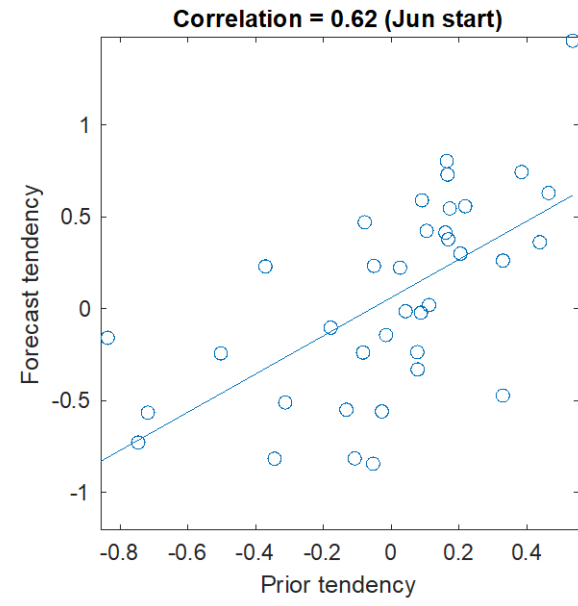
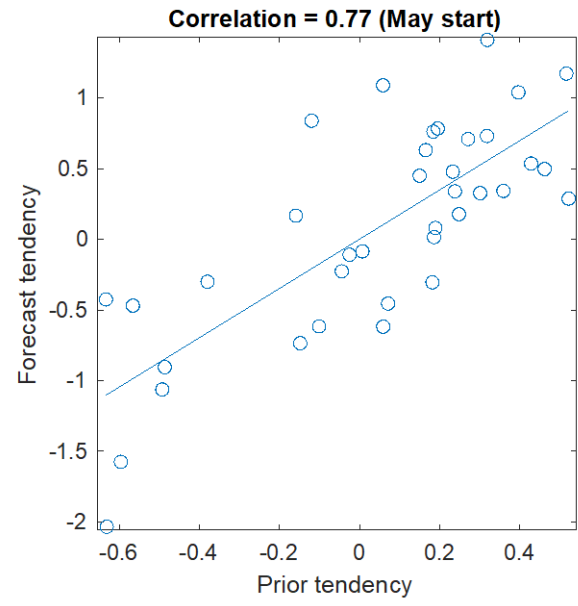
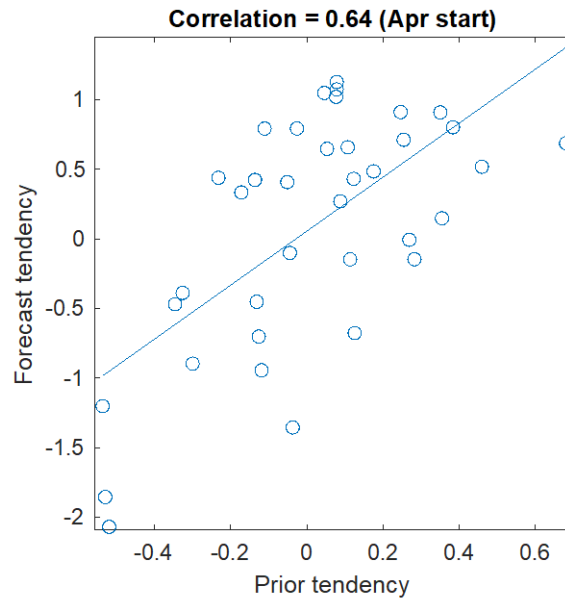
For each month of the year, we can define the **ENSO momentum** as the correlation between the *prior* tendency and the *subsequent* tendency

Observations
Forecasts

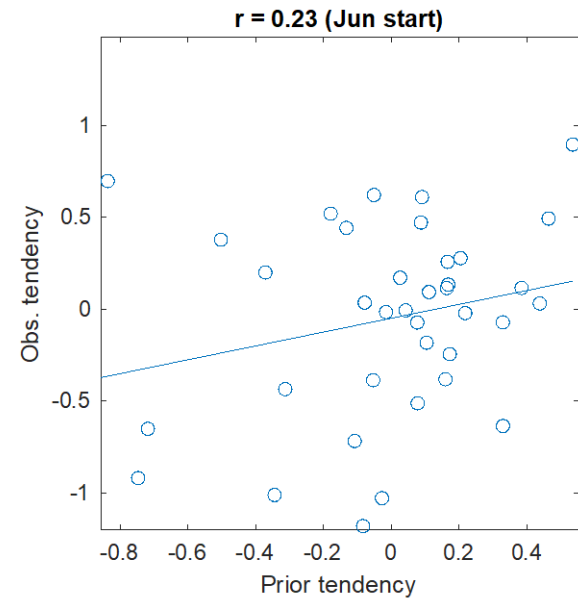
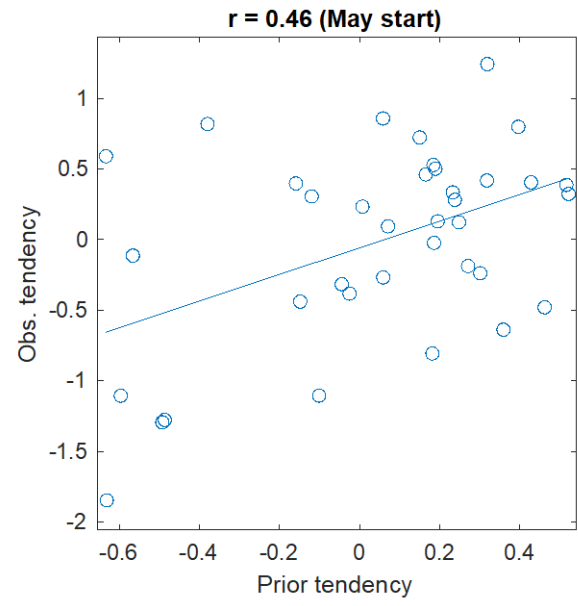
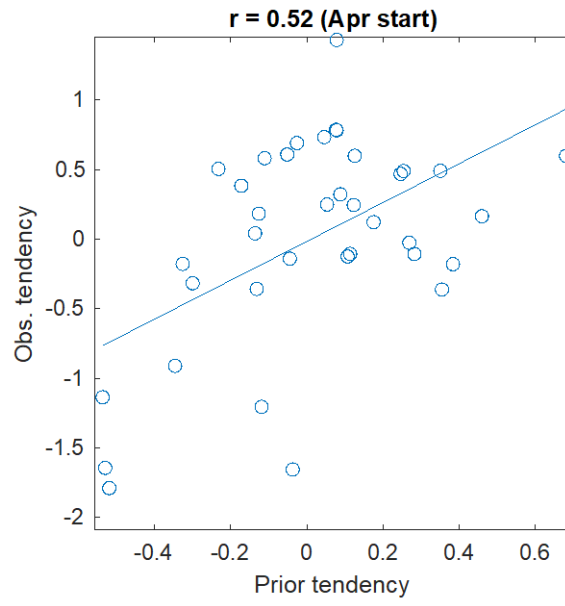


Correlation
between Mar—Apr
and May—Aug
tendencies

ENSO Momentum

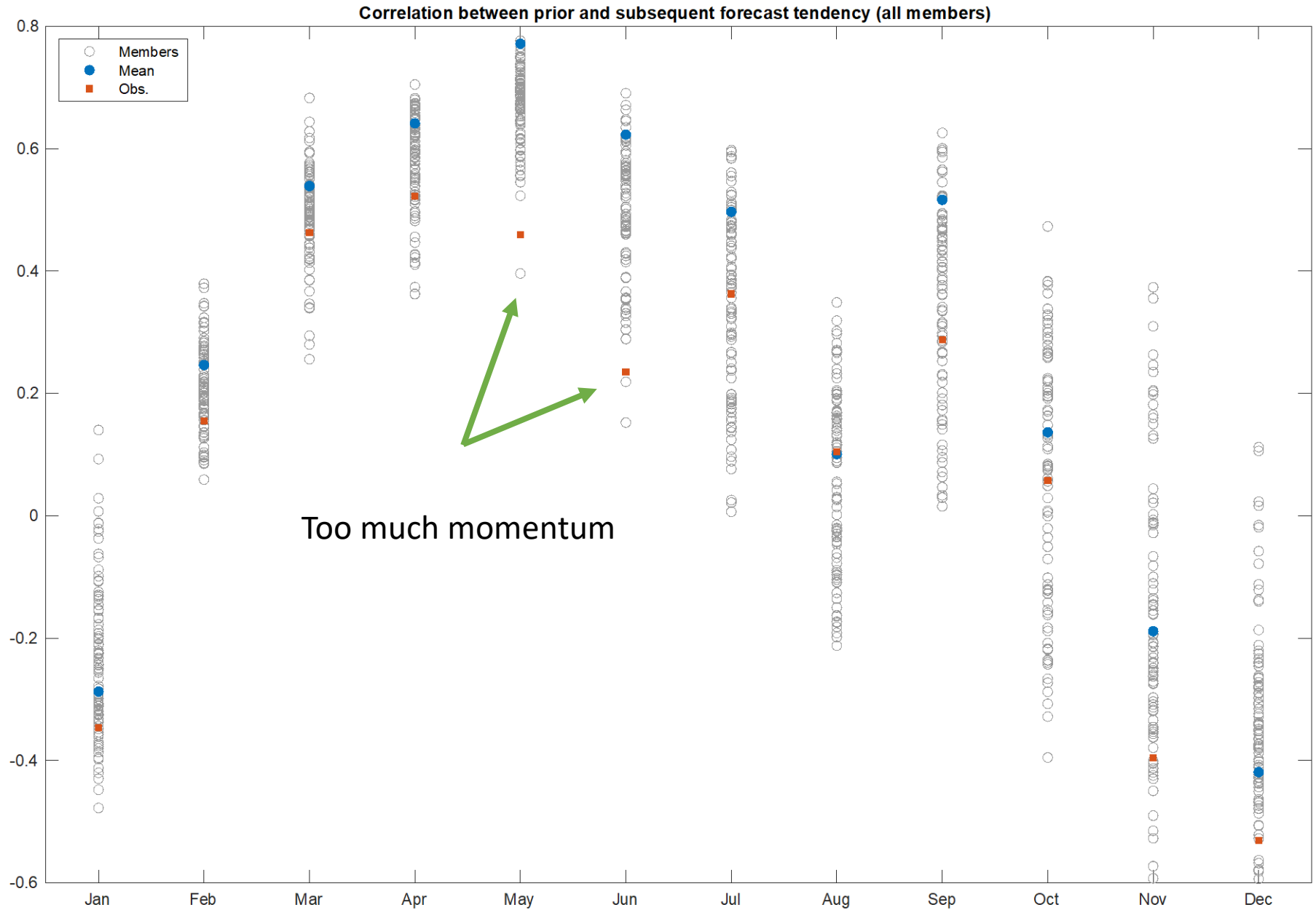


**Ensemble-mean
forecasts**



Observations

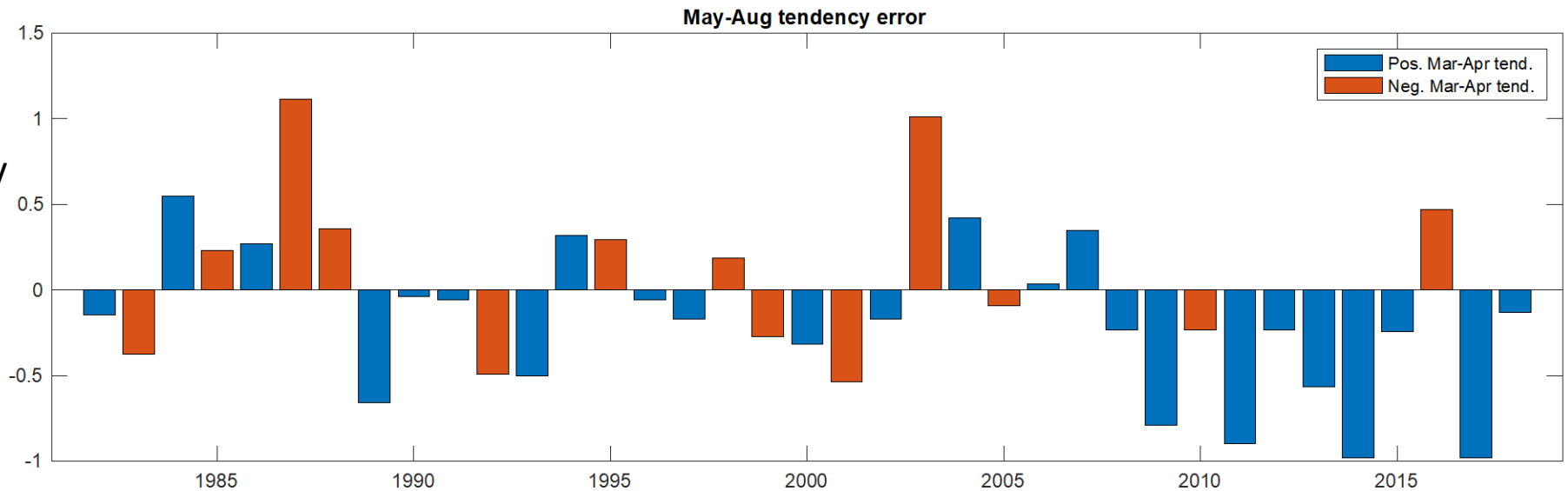
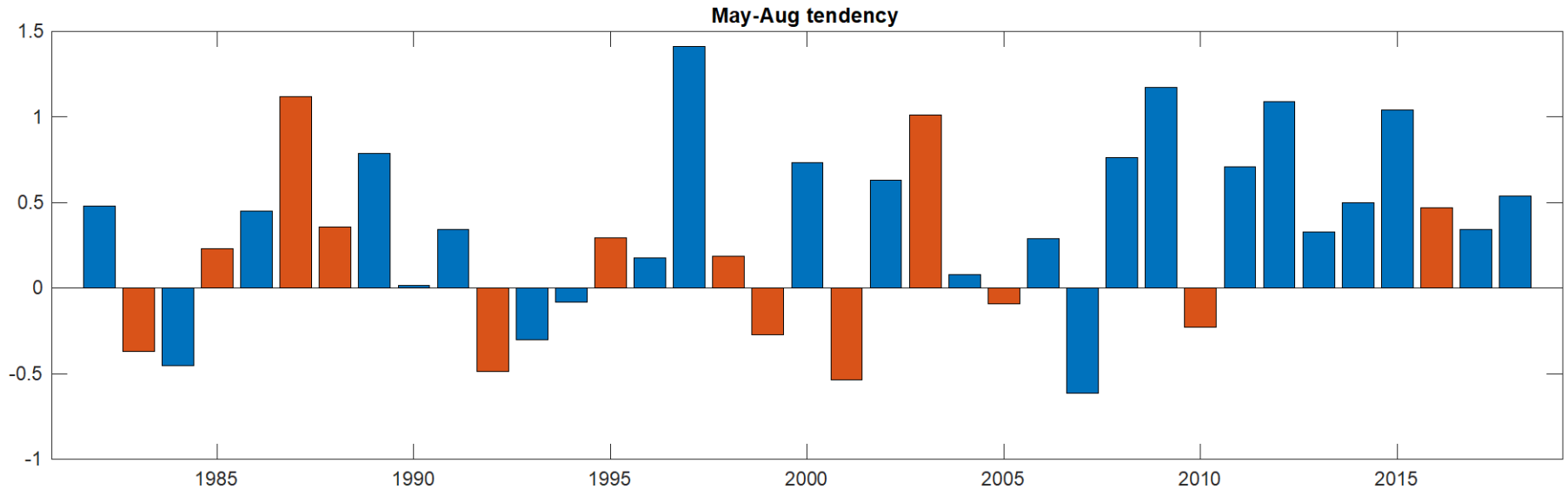
ENSO momentum in
observations and
ensemble members



State-dependent forecast errors

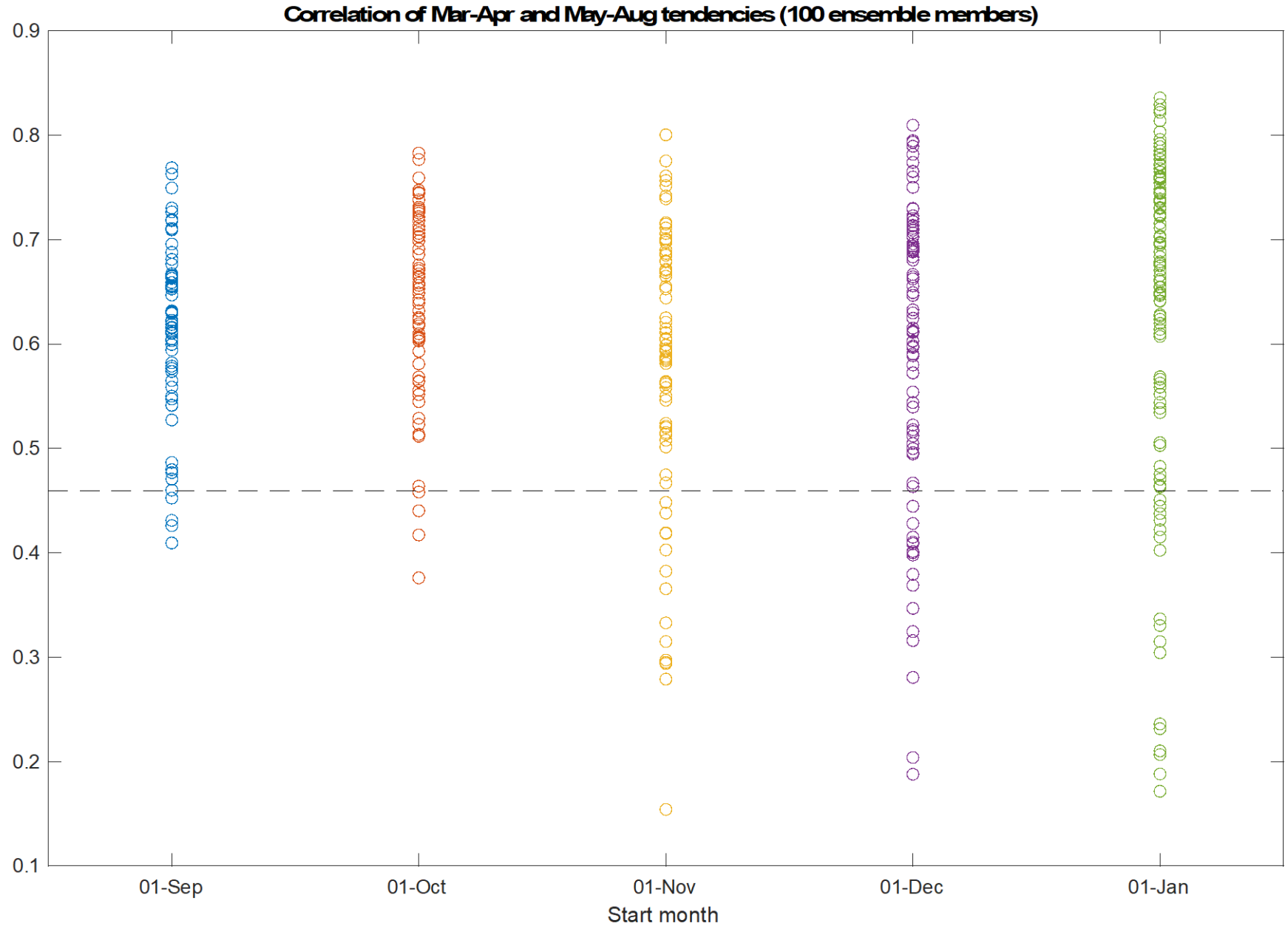
1. Prior tendency is **positive**.
2. The forecast tendency is likely positive.
3. The observation not as likely to be positive.
4. The tendency error (obs-forecast) is likely to be negative

Correlation of prior and forecast error = -0.55



Initialization problems?

Earlier starts also have too much momentum.
Initialization not entirely to blame.



Could check in free running model.

Linear algebra!

All of the time structure, including "momentum" is in a covariance matrix

- Cut the Nino 3.4 times series into 12-month segments
- Put each segment into the column of a matrix X
 - X has 12 rows
 - Row 1 is all the January values
 - Row 2 is all the February value
 - And so on
 - The number of columns = # years
- $C = XX^T / (\text{number of years} - 1)$

Datum / Date:

Everything is in the covariance matrix

Arrange the data (obs) in a $12 \times \# \text{ years}$ matrix. X.

$$X = \begin{bmatrix} J & J & \dots & J \\ F & F & \dots & F \\ \vdots & \vdots & \dots & \vdots \\ D & D & \dots & D \\ 1982 & 1983 & \dots & 2018 \end{bmatrix}$$

Apr/May tendency = $d_1^T X$ with

$$d_1 = \begin{bmatrix} 0 \\ 0 \\ -1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$\begin{matrix} 1 \times 12 & 12 \times 37 \\ \uparrow & \uparrow \\ & 1 \times 37 \end{matrix}$

Aug/May tendency = $d_2^T X$

$$d_2 = \begin{bmatrix} 0 \\ 0 \\ 0 \\ -1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

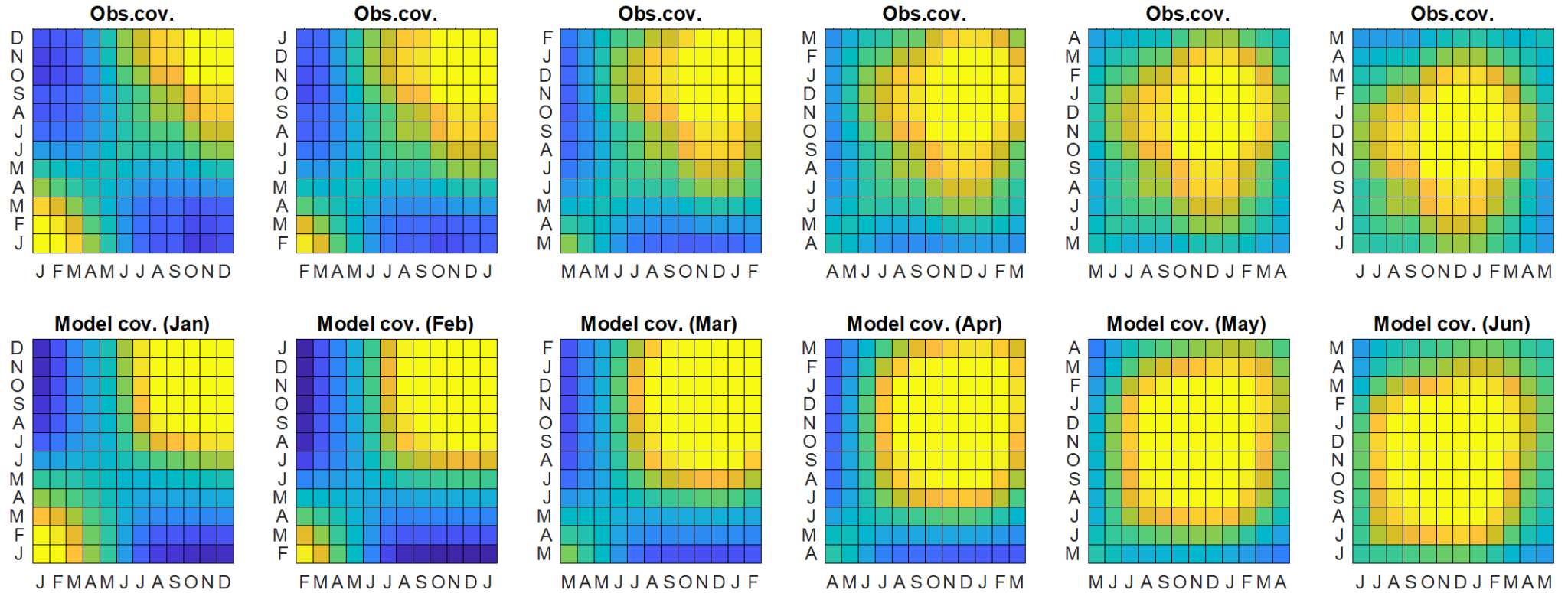
Correlation of Apr/May & Aug/May is

$$\frac{d_1^T X (X^T X)^{-1} X^T d_2}{\sqrt{(d_1^T X (X^T X)^{-1} X^T d_1) (d_2^T X (X^T X)^{-1} X^T d_2)}} = \frac{d_1^T X X^T d_2}{\sqrt{(d_1^T X X^T d_1) (d_2^T X X^T d_2)}}$$

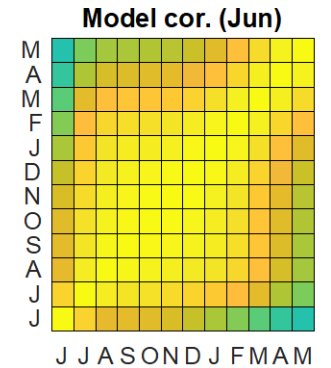
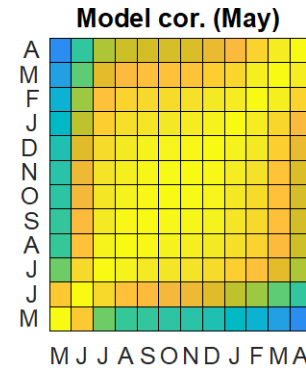
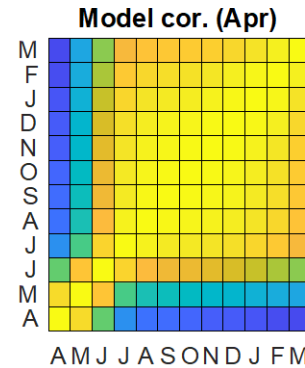
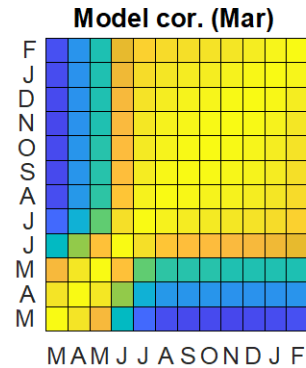
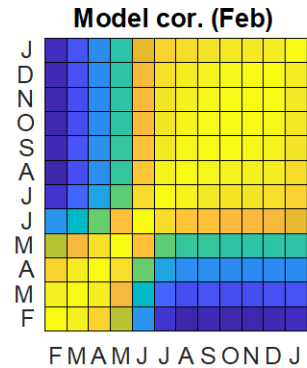
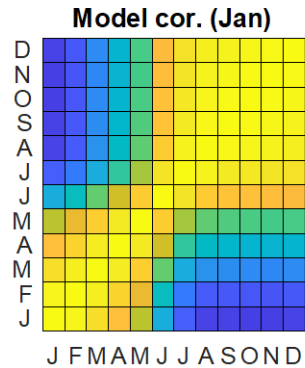
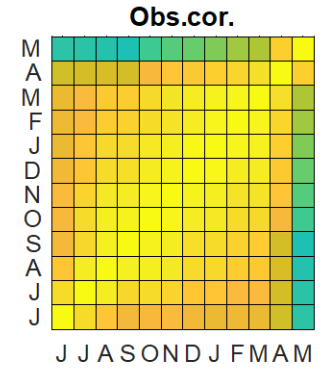
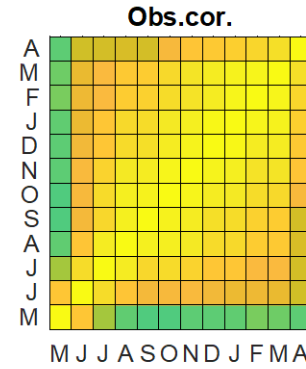
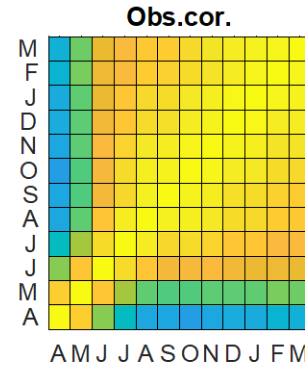
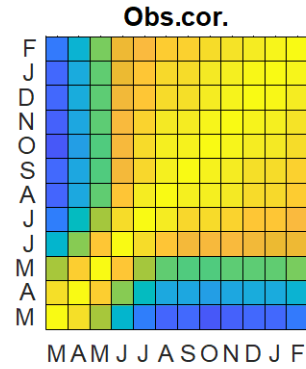
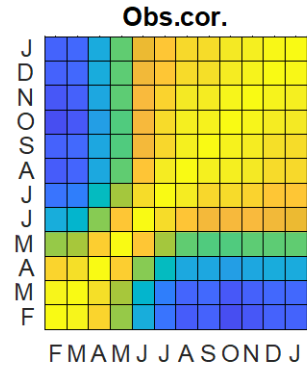
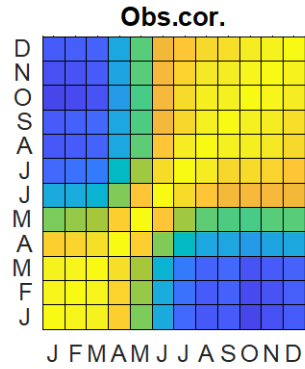
$$= \frac{d_1^T C d_2}{\sqrt{(d_1^T C d_1) (d_2^T C d_2)}}$$

with $C = \frac{1}{37-1} X X^T$
Covariance

We can look at covariance matrices ...

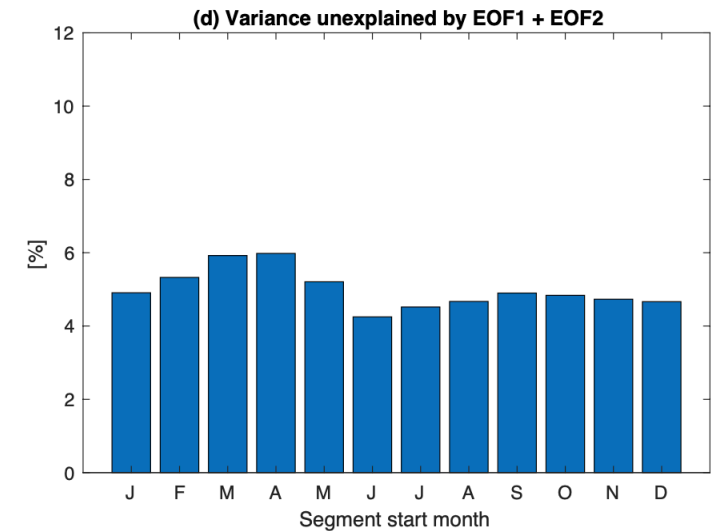
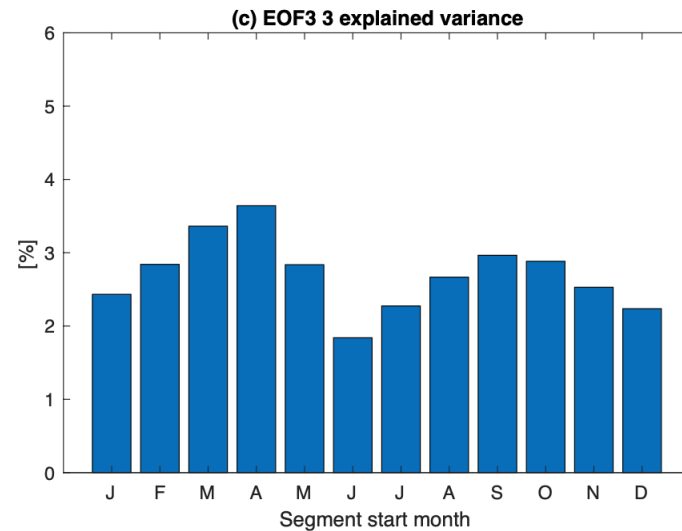
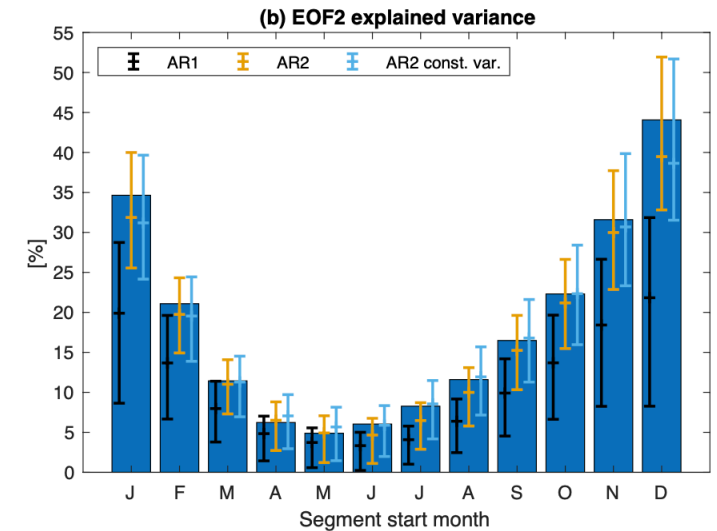
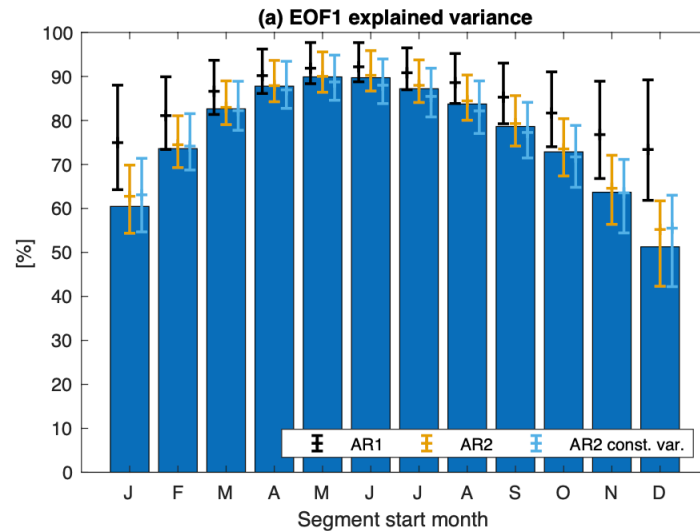


We can look at correlation matrices ...

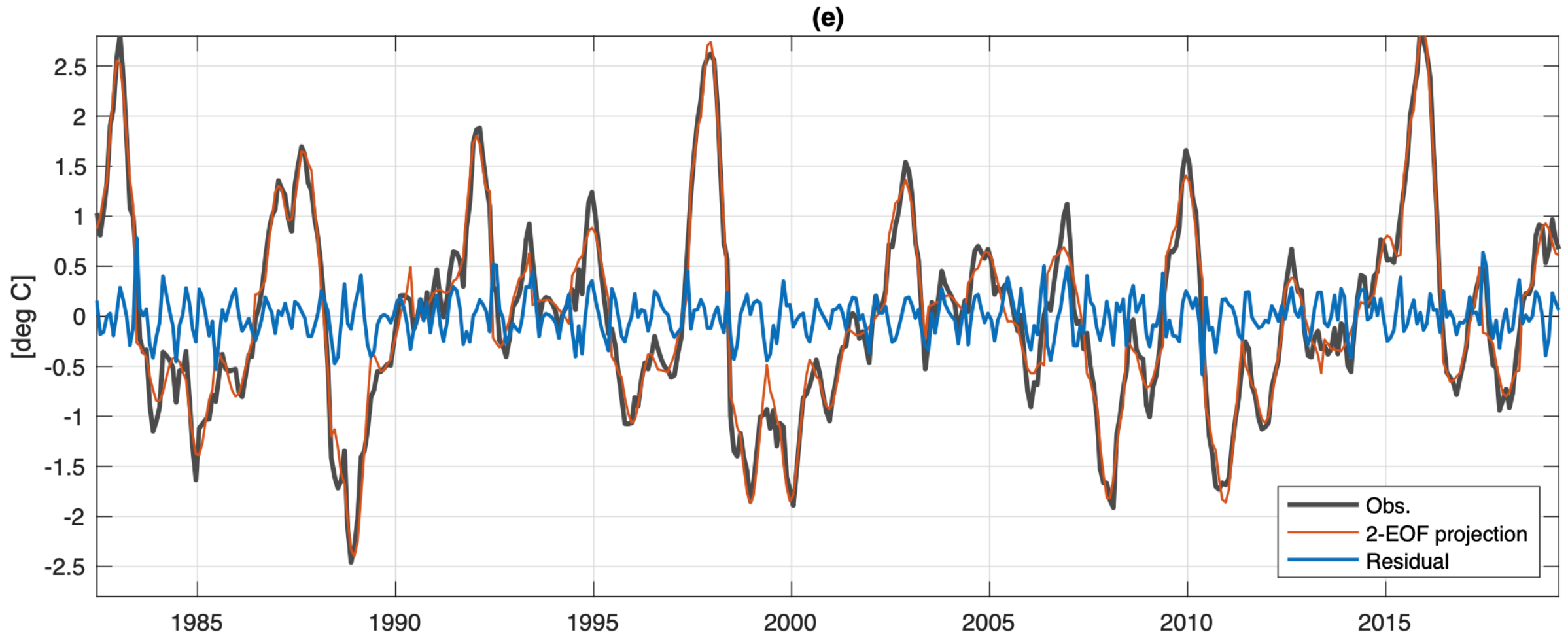


Luckily they are low-dimensional!

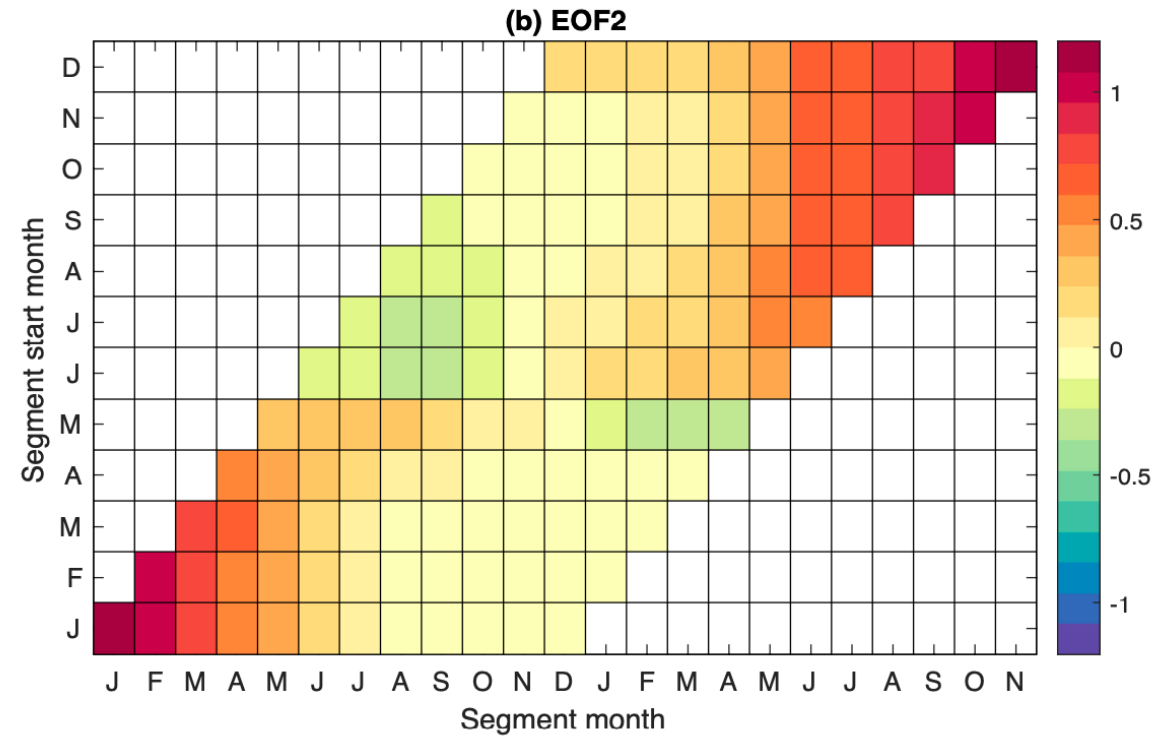
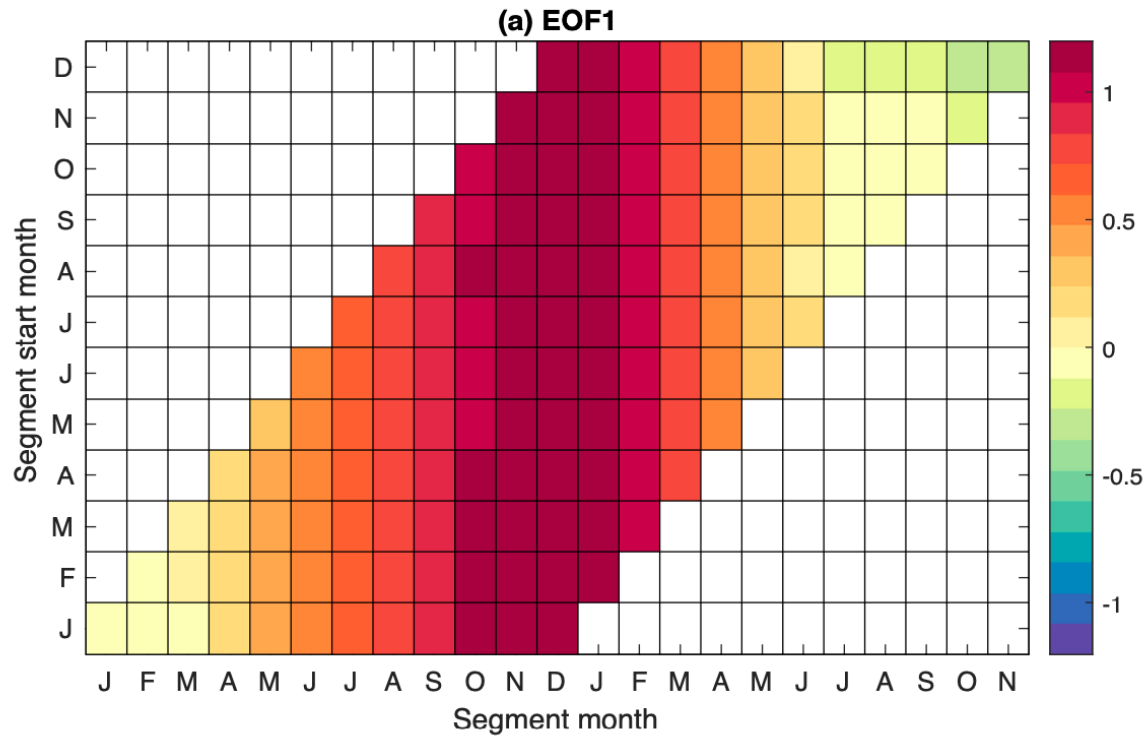
2 EOFs explain close to 95% of the variance



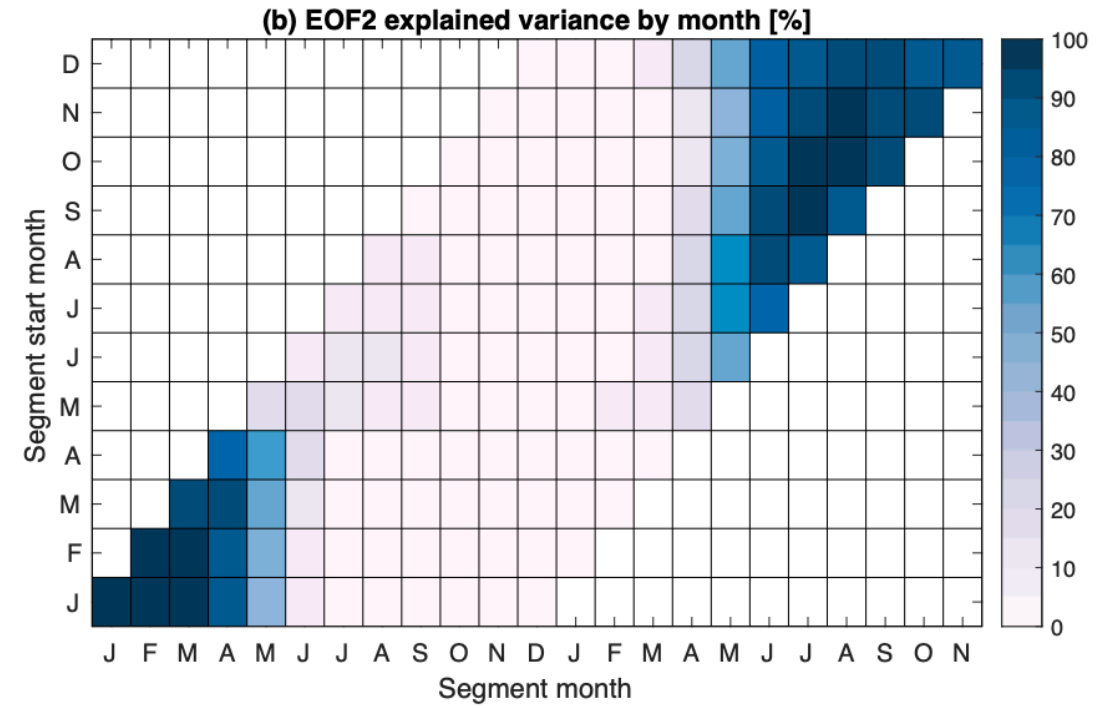
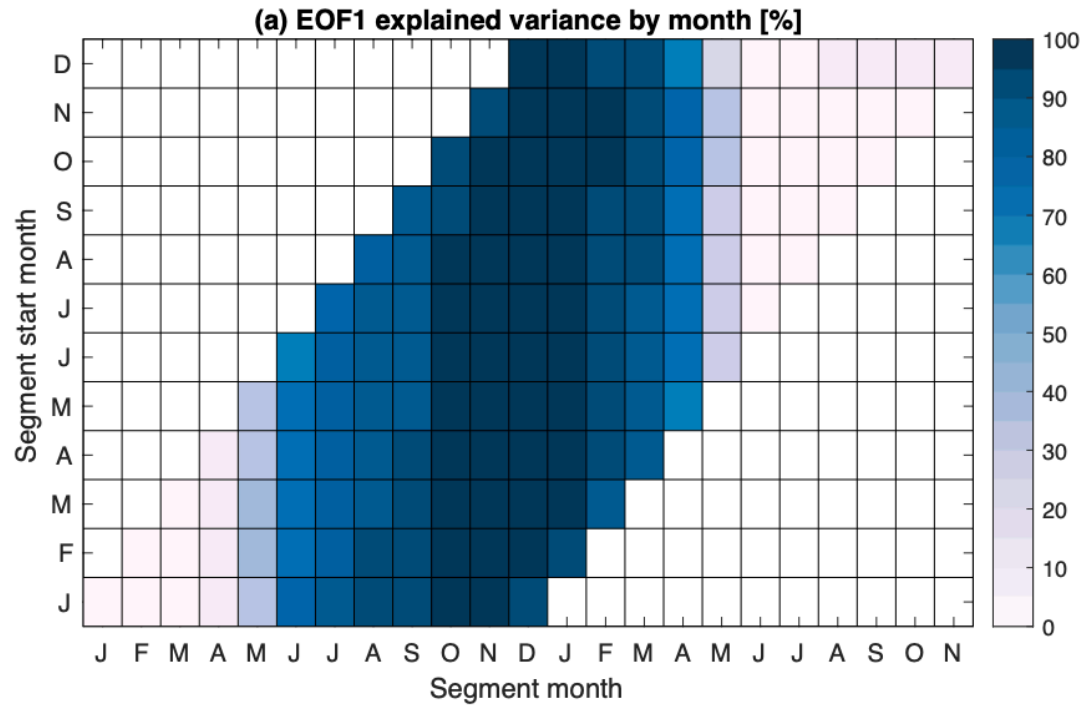
Approximation of Nino 3.4 using 2 EOFs



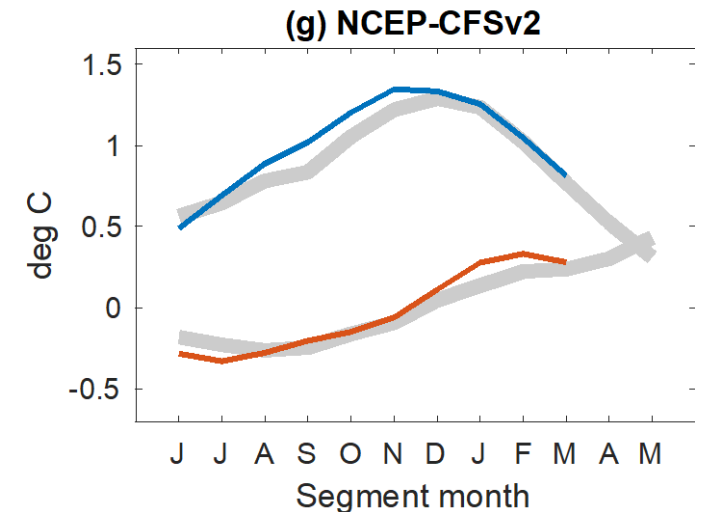
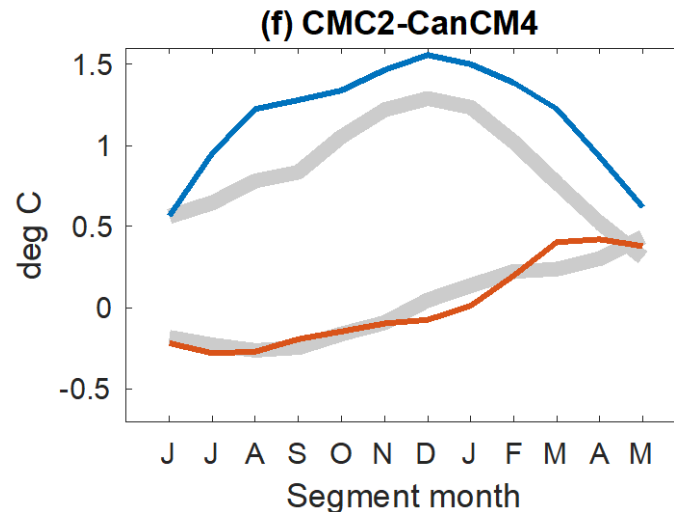
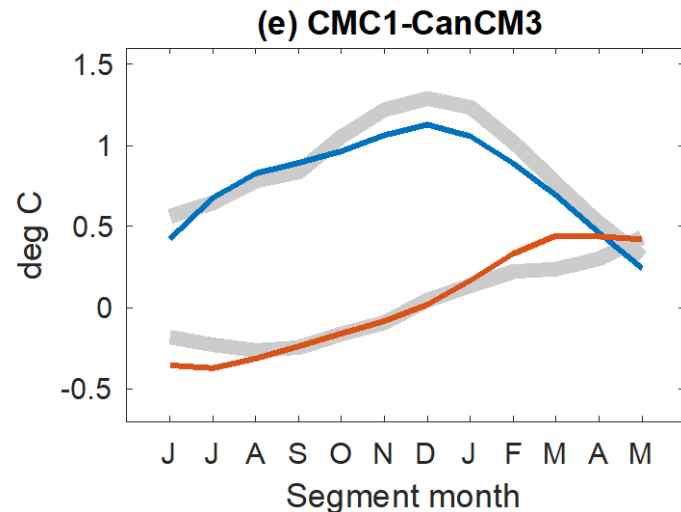
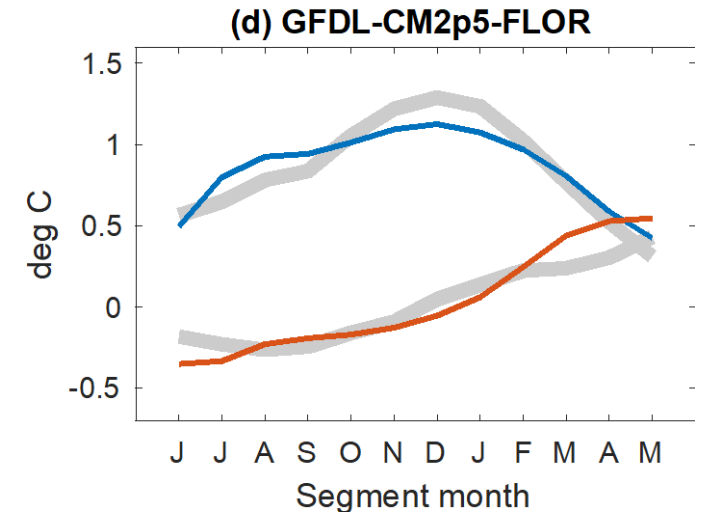
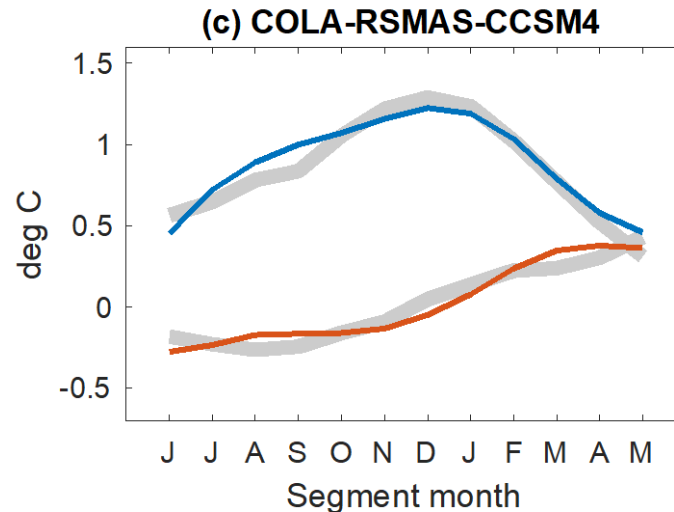
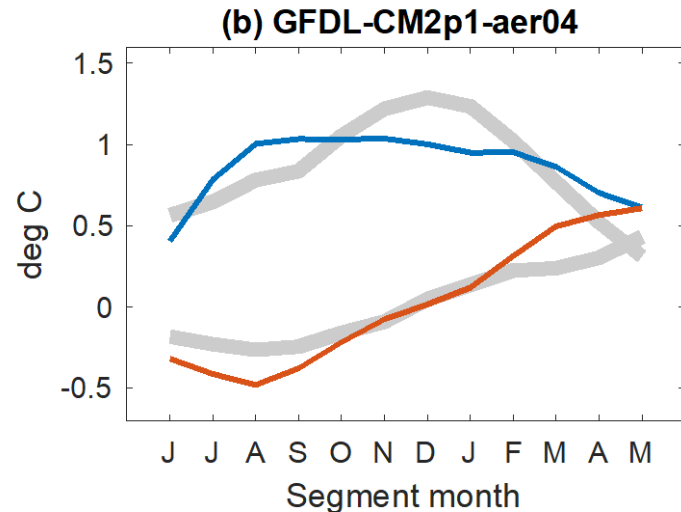
What do the EOFs look like?



Variance explained

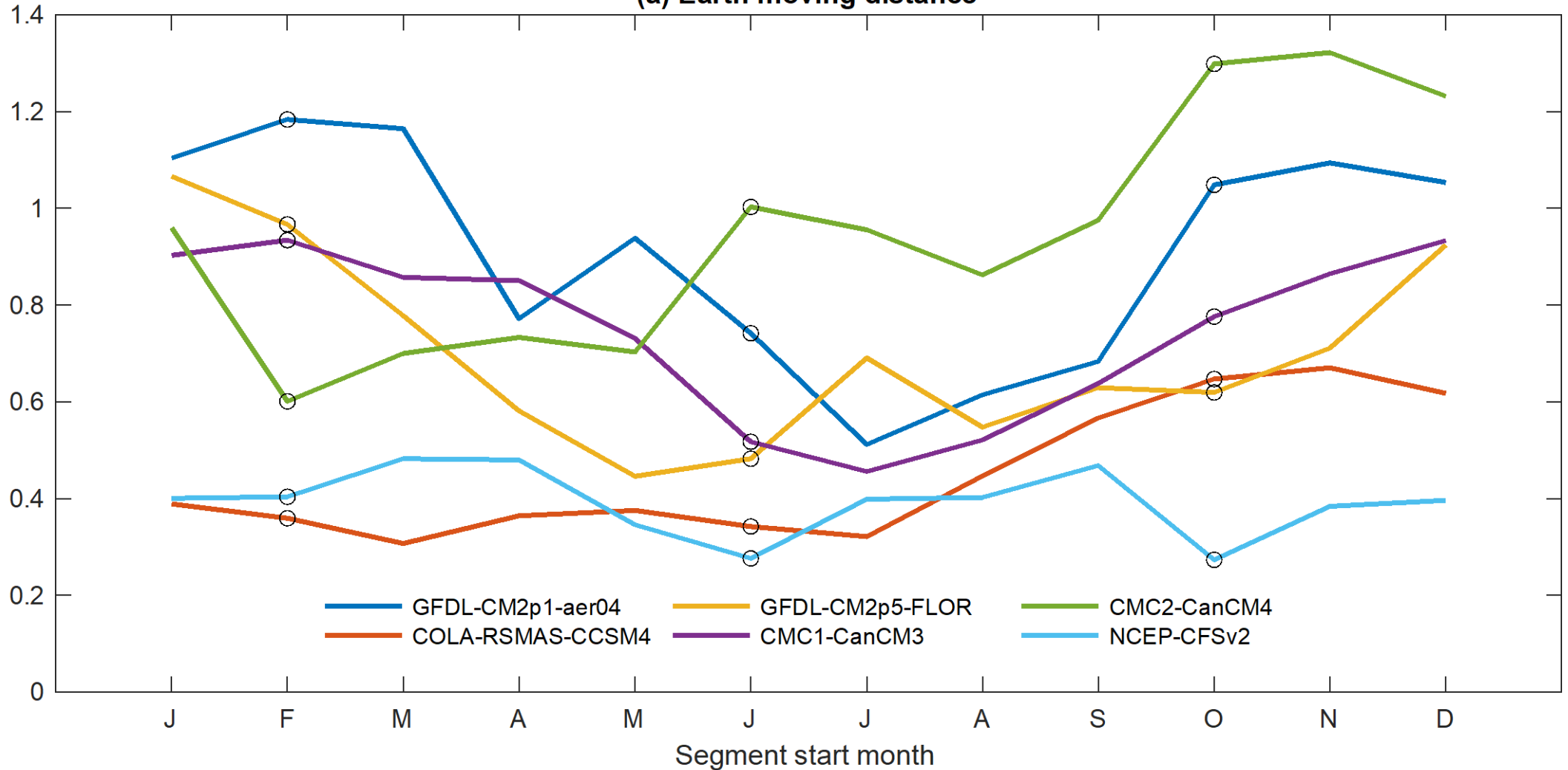


Back to forecasts. Compare EOF of forecasts and observations

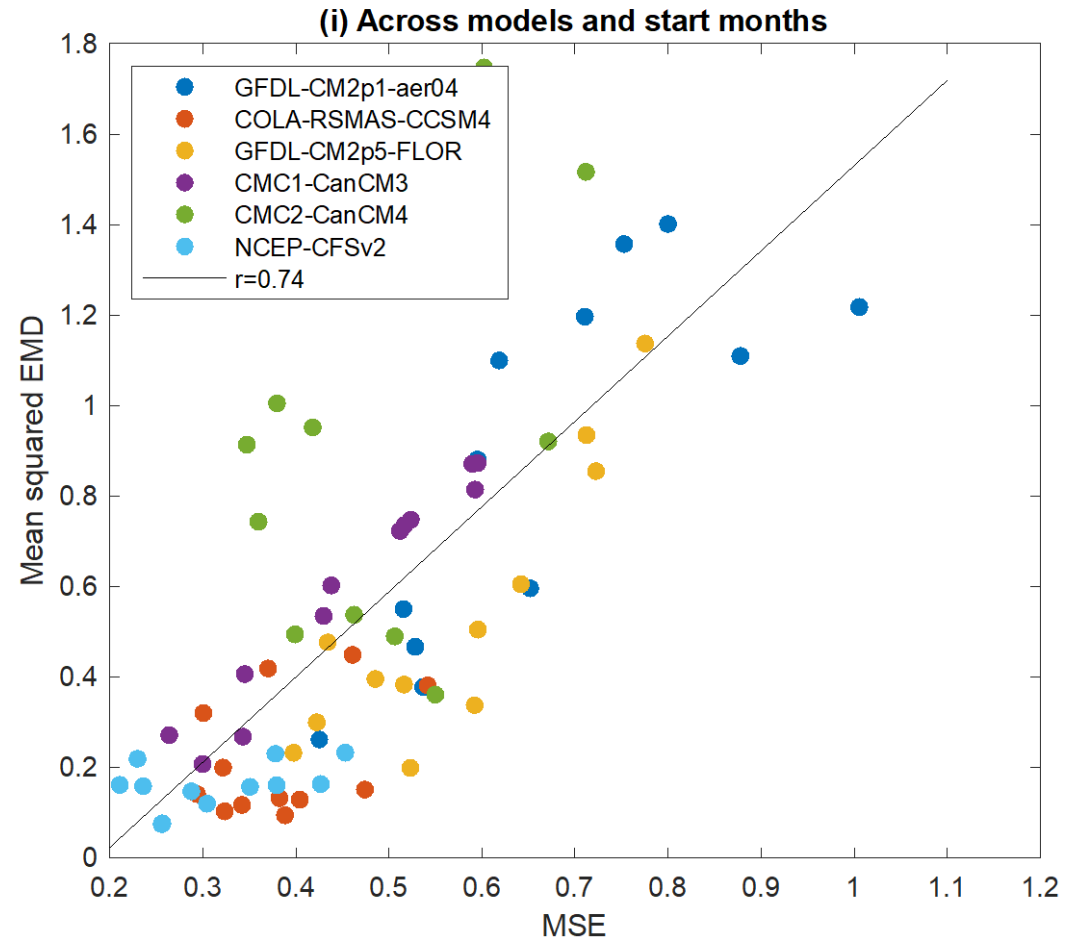
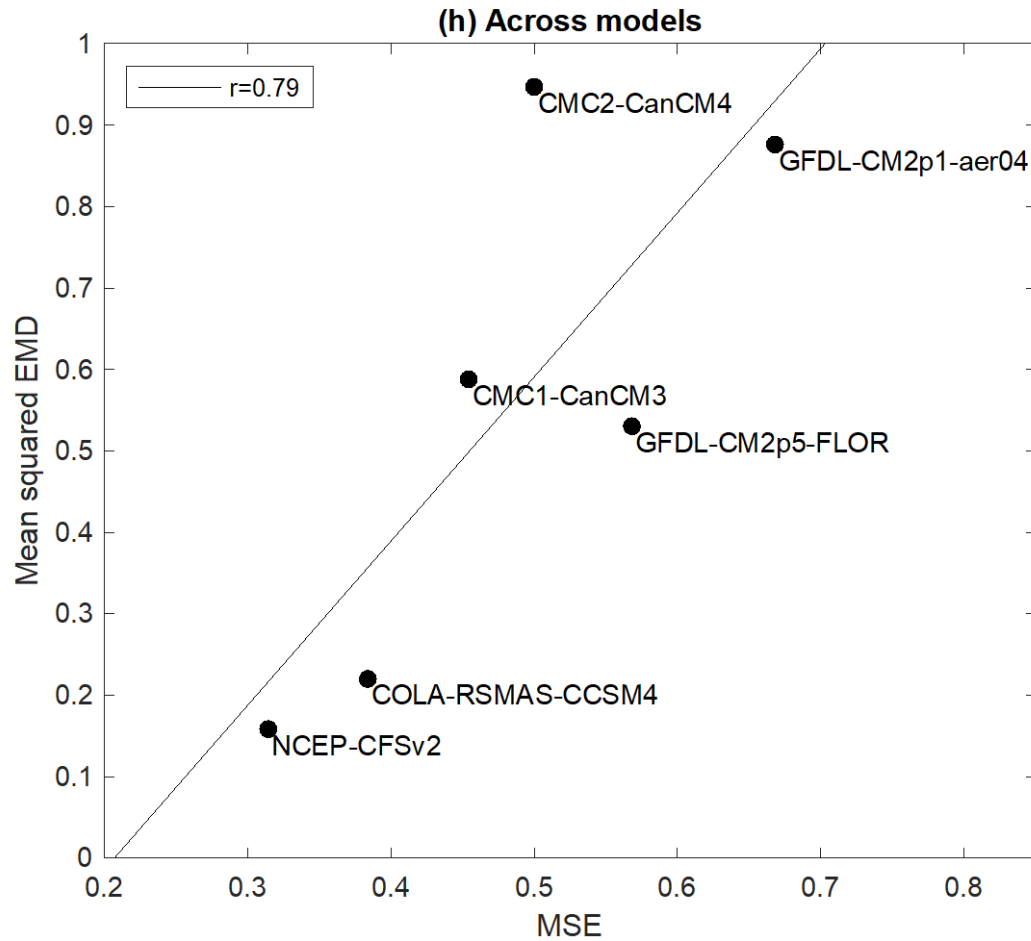


EMD measures distance between models and observed covariance

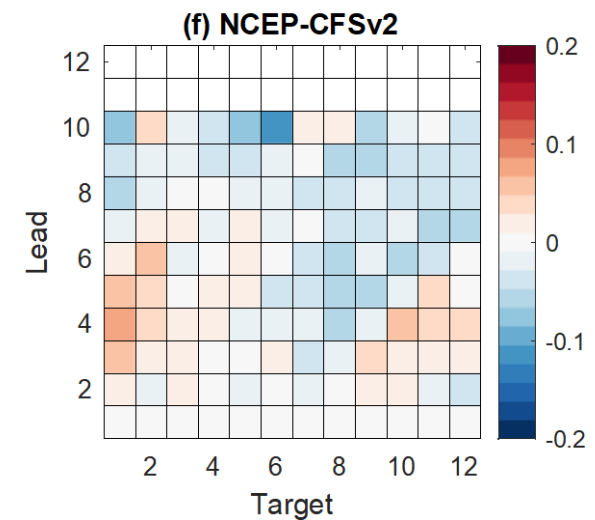
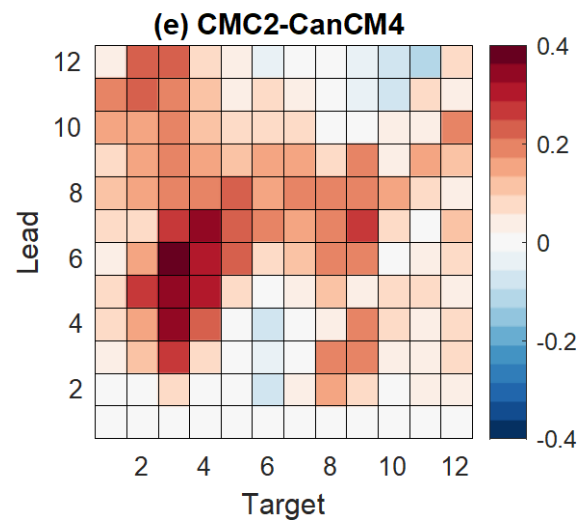
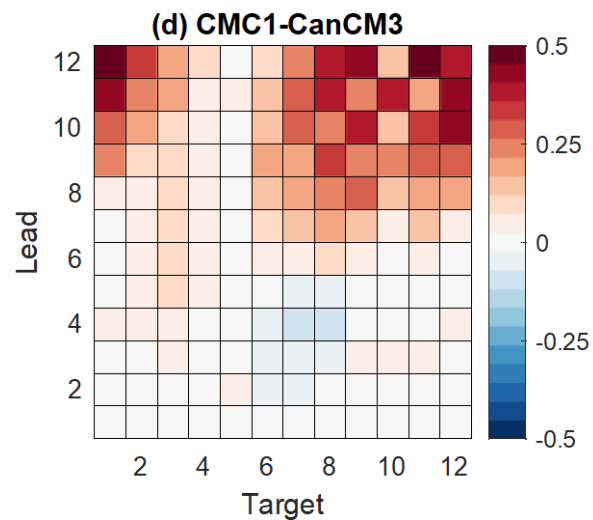
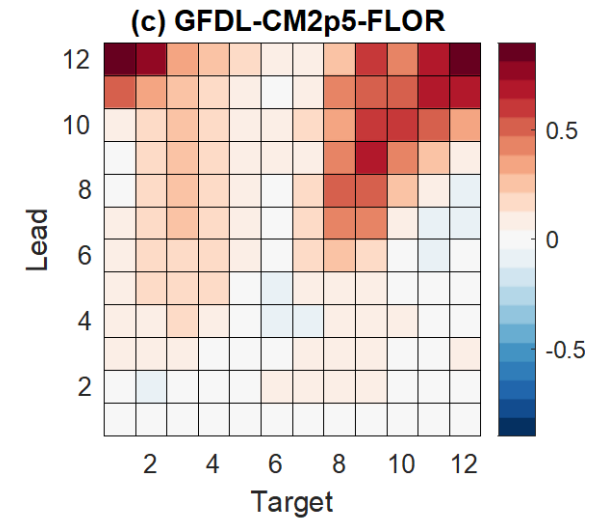
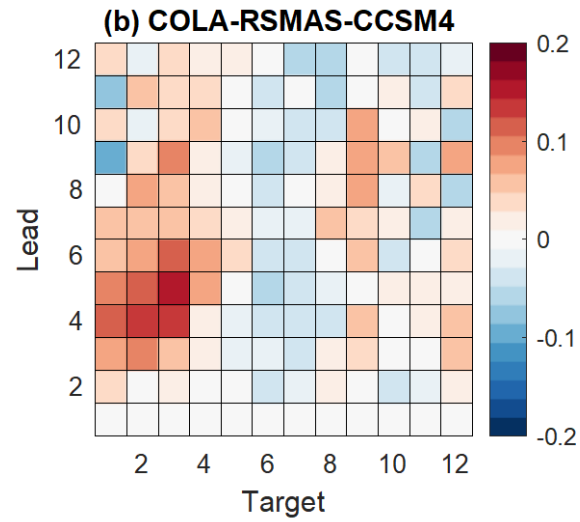
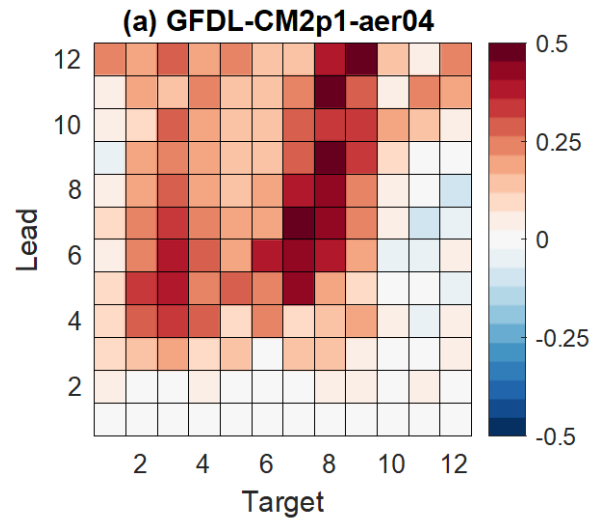
(a) Earth moving distance



Models with better covariances have lower MSE



EOFs can be used in a regression to reduce mean-squared error



Summary

- Late-spring ENSO *forecasts errors* depend on the observed ENSO tendency before the forecast.
 - “Momentum” = ENSO tends to keep going in the same direction
 - Models have state-dependent errors
- Consequence: Late-spring ENSO forecasts are unreliable.
- Are model dynamics or initialization to blame?
 - Some evidence for dynamics being the culprit
- EOF analysis shows ENSO time structure is 2-dimensional
 - Models with better time structure have smaller errors.
 - EOF-based regression reduces forecast MSE